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Stock Prediction via Linear Regression and BP Regression Network

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Abstract: Stock prediction is an important and challenging problem. In this paper, two models, i. e., a multiple linear regression based model and a BP neural network based model were studied to predict the movements of the stock market. Through the analysis of the conceptual topic index of Shenzhen A-share "Gree Electric Appliances" (000651) and the prediction of stock price technical indicators on opening price of the next day, it was found that the results predicted by technical indicators on the

opening price were more accurate than the conceptual topic index. At the same time, we compared
 the fitting degree, simulation and prediction ability of the multiple linear regression model and the

⁵ BP neural network prediction model. The results show that the prediction model based on BP neural

⁶ network works better than the multiple linear regression model. We trained and tested the index of

⁷ "Gree Electric Appliances" in 220 trading days in this paper. Based on the experimental results, the

⁸ conclusion was drawn that the BP neural network based model with the stock technical index as the

° characteristic variable can predict the movements of the stock market well.

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- ¹¹ **Keywords:** BP neural network; linear regression; stock price prediction; R language
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14 1. Introduction

The stock market is a "high income with high risks" investment field. Countless experts and scholars are constantly looking for effective analytical methods and models to find out the laws of stocks and predict stock [1–5]. Nowadays, a popular research method is to apply a neural networks to prediction [6–9]. The efficiency of neural network model is often superior to multivariate statistics, which is relatively outdated [10–15]. Most previous work adopts various technical indicators of stocks as characteristic variables, while the price at a certain moment or the average price of a certain period of time is the response variable, and the accuracy of various forecasting results are compared.

However, each stock has its own "conceptual topic", and the trend of "conceptual topic" can also reflect the development and popularity of the stock. A stock generally belongs to several conceptual topics. *If the index of the conceptual topics are used as characteristic variables, can we predict the trend of stocks*? The problem has been rarely studied in this area. In this paper, we first use iterative algorithm

to find out the best number of hidden layers applicable for a set of stock data. Then the multiple

regression[16–19] and BP neural network [20–27] were used to predict the opening price of the second
 trading day, with technical indicators and the conceptual subject index as the characteristic variables.

²⁹ Finally, the pros and cons of four methods are shown through prediction results.

30 2. Preliminaries

31 2.1. Multiple linear regression

Multiple linear regression model is a popular regression analysis method exploiting the linear relationship between an observed variable and multiple input variables. The general form of multiple linear regression model is as follows:

$$y = \beta_0 + \beta_1 x_1 + \beta_2 x_2 + \dots + \beta_p x_p + \varepsilon \tag{1}$$

where $y \in \mathbb{R}$ is the observed variable; x_i $(i = 1, 2, \dots, p)$ are the input variables; $\beta_0, \beta_1, \dots, \beta_p$ are the unknown parameters; and ε is a zero-mean random Gaussian noise with variance σ^2 . For notation simplicity, let $x = (x_1, \dots, x_p)' \in \mathbb{R}^p$ be the collection of input variables and $\beta = (\beta_1, \dots, \beta_p)' \in \mathbb{R}^p$ be the coefficient vector to be estimated.

Suppose we have *n* observations y_1, \dots, y_n with input variables x_1, \dots, x_n and noise $\varepsilon_1, \dots, \varepsilon_n$. Representing Eq. (1) in matrix form, we obtain

$$Y = X\boldsymbol{\beta} + \boldsymbol{\varepsilon} \tag{2}$$

- where $Y = (y_1, \dots, y_n)' \in \mathbb{R}^n$ is the observation vector, $X = (x_1, \dots, x_n)' \in \mathbb{R}^{n \times p}$ is the matrix of input variables, and $\varepsilon = (\varepsilon_1, \dots, \varepsilon_n)' \in \mathbb{R}^n$ is the noise vector.
 - In Eq. (2), if *X* is a column full rank matrix, by applying the least-squares estimation, the estimation of β is

$$\hat{\boldsymbol{\beta}} = (X'X)^{-1}X'Y \tag{3}$$

With the estimation $\hat{\beta}$, and the regression result y_{new} of a new input vector x_{new} is given by the sample regression function as follows:

$$y_{\text{new}} = x'_{\text{new}}\hat{\beta} \tag{4}$$

- ³⁸ The sample regression function (4) needs to be further statistically tested to determine the reliability of
- the estimation, including the F-test of the regression equation, the regression coefficient t-test, and test of fitness of the regression.
- The F test of the significance of the regression equation
- ⁴² H₀:Original hypothesis is tenable
- ⁴³ H₁:Original hypothesis is not tenable

If the assumption of is tenable, then

$$F = \frac{\frac{SSR}{p}}{\frac{SSE}{(n-p-1)}}$$
(5)

44 where $F \sim F(p, n-p-1)$, $SSR = \sum_{i=1}^{n} (\hat{y}_i - \bar{y})^2$, $SSE = \sum_{i=1}^{n} (y_i - \hat{y}_i)^2$. Given the level of

significance α , check the table to get the critical value $F_{\alpha(p,n-p-1)}$, and calculate the value of F from a

sample. If $F > F_{\alpha(p,n-p-1)}$, then reject (or accept) in the opposite case H_0 , to determine whether the

- ⁴⁷ linear relationship of the original equation is significant.
- t-test of regression coefficient

Structure t Statistics

$$t_i = \frac{\hat{\beta}_i}{\hat{\sigma}\sqrt{c_{ii}}} \sim t \left(n - p - 1\right) \tag{6}$$

where $\hat{\sigma} = \sqrt{\frac{SSE}{n-p-1}}$. Given a significant level α ,get the critical value $t_{\frac{\alpha}{2}}(n-p-1)$. According to $|t_i| > t_{\frac{\alpha}{2}}(n-p-1)$ to decide (or accept) the null hypothesis H_0 ,then to determine whether the corresponding explanatory variable should be included in the model.

• Test of fitness of the regression

$$R^2 = \frac{SSR}{SST} = \frac{SSR}{SSR + SSE} \tag{7}$$

In the formula, R^2 is the determined coefficient of the sample. The closer the statistic is to 1, the higher the goodness of fit of the model.

54 2.2. BP neural network

The BP algorithm^[28] was proposed by a group of scientists led by Rumelhart and McCelland in 55 1986. It is a multi-layer feedforward network trained by error inverse propagation algorithm and is one 56 of the most widely used neural network models. The BP algorithm consists of two parts: the forward 57 propagation of the signal and the back propagation of the error. In the forward propagation process, 58 the signal is transmitted from the input layer of the network to the output layer through the hidden 59 layer layer by layer, and the actual output of the network is obtained. If the actual output does not 60 match the expected output, then the error back propagation phase is entered. In the back propagation 61 phase, the output error is transmitted back to the input layer via the hidden layer, thereby obtaining an 62 error signal of each unit of each layer, and the network connection weight is adjusted according to the 63 signal. The two processes of forward propagation of the signal and back propagation of the error are 64 repeatedly performed until the network output error is less than a predetermined threshold or until a 65 predetermined study number of times is performed. 66

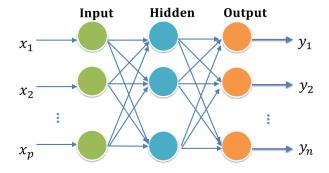


Figure 1. Structure of BP network

⁶⁷ Suppose that we study the lth layer of neurons j, i represent the (l-1)th layer of neurons and k ⁶⁸ indicates l+1 layer of Then o_j representing the output of neurons j, ω_{ji} representing the connection ⁶⁹ weight between neurons i and j, ω_{ik} representing the connection weight between neurons j and k.

⁷⁰ The steps of BP neural network algorithm :

- 1. Initialize all network weights $\omega_{ki}(t)$ (including bias) is a small random number, where t indicates the number of learning steps and is initialized to 0.
- 73 2. Repeat the follow process until convergence (calculated each training sample).
 - Forward propagation of the signal.Calculate the output *o_j* of each hidden layer and output layer neurons layer by layer:

$$net_j = \sum_i \omega_{ji} (t) o_i \tag{8}$$

$$o_j = f\left(net_j\right) \tag{9}$$

In the formula, $f(\cdot)$ is an activation function. Use the Sigmoid function as the activation function:

$$o = f(net) = \frac{1}{1 + e^{-net}}$$
 (10)

• The direction of the error propagates.

First, calculate the neurons in the output layer.

$$\delta_j = (d_j - o_j) o_j (1 - o_j) \tag{11}$$

In the formula, δ_j is the error signal, d_j is the desired output, and o_j is the actual output. Then calculate the neurons of each hidden layer along the network.

$$\delta_j = o_j \left(1 - o_j \right) \sum_k \omega_{kj} \delta_k \tag{12}$$

If j is the first l layer of neurons, in the above formula ∑ is the summary of all neurons k of l+1 layer.
Calculate the weight correction amount:

$$\Delta \omega_{ji}\left(t\right) = \eta \delta_{j} o_{i} \tag{13}$$

• Update each network weight:

$$\omega_{ji}\left(t+1\right) = \omega_{ji} + \Delta\omega_{ji}\left(t\right) \tag{14}$$

77 3. Data Acquisition

"Gree Electric Appliances" is a typical stock representing China's manufacturing industry. It is
a conceptual stock with a lot of topics. This experiment predicts the opening price of Gree Electric
Appliances by analyzing the concept theme index and stock price technical indicators of it. For the
sake of generality, make use of the 220 sets of data from 5 August 2017 to 11 July 2018 when exploring
the next day's opening index.80% of them were randomly selected as network training data, and the
restwas used as test data to verify the accuracy of the BP network. The training data of groups is 176
and the test data is 44.

The main conceptual topics belonging to "Gree Electric" include the ten concept themes of 85 state-owned enterprise reform, smart home, MSCI China, new energy, low-carbon economy, new energy vehicles, margin trading, electrical machinery, industry 4.0, and social security. The indices of 87 the ten subjects are set to x_1 , x_2 , x_3 , x_4 , x_5 , x_6 , x_7 , x_8 , x_9 , and x_{10} as the first set of characteristic variables 88 respectively. In addition, the traditional stock technical indicators include the volume, the number of 89 transactions, K, D, J, MACD, BIAS1, BIAS2, BIAS3, and the average volume of the transaction volume. 90 Similarly, these ten indicators are set to x_1 , x_2 , x_3 , x_4 , x_5 , x_6 , x_7 , x_8 , x_9 , x_{10} which are used as the second 91 set of characteristic variables. Among them, the transaction volume refers to the total number of shares 92 traded on the same day (1 lot = 100 shares), the number of transactions refers to the number of pending 93 orders of all traders, and the KDJ indicator is calculated based on the highest price, the lowest price 94 and the closing price. The K value, D value and J value, the three can accurately reflect the price 95 fluctuation trend and its strength, generally used to predict the short- and medium-term market. The 96 MACD is an exponentially smooth moving average that characterizes the current long-short state and 97 possible trends in stock prices. BIAS is a technical indicator that reflects the degree to which the stock 98 price deviates from the moving average during the volatility process. It judges the timing of buying 99 and selling by calculating the percentage of the stock price that deviates from the moving average. 100 These technical indicators are the most basic and most representative of the stock price trend. 101 In order to compare the predictive performance of multiple regression and BP neural network 102

on stock price, the next-day opening price of Gree Electric Appliance is taken as the one-dimensional
 response variable of the final output.

Normalization and anti-normalization To eliminate the difference in magnitude between data, the input methodshould first be normalized. The normalization formula is as follows:

$$x' = \frac{x - \min(x)}{\max(x) - \min(x)}$$
(15)

However, the computing result (predicteddata) is all between 0 and 1,anti-normalizationmethod should be applied to reset the results to the magnitude of actual data. The anti-normalization formula is as follows:

$$x' = x_{result} \left(max \left(x \right) - min \left(x \right) \right) + min \left(x \right)$$
(16)

The hidden layer number of BP neural network has a great influence on the accuracy of network prediction. In this experiment, the change of prediction accuracy is observed by changing the number of hidden layers. We found out that when the network has 5 or 7 hidden layers, the correlation coefficient between predicted and actual data reach the highest point, which means that prediction accuracy is relatively higher. However, a network with too many hidden layers may cause "over-fitting" phenomenon, so we only established a BP network with 5 layers.

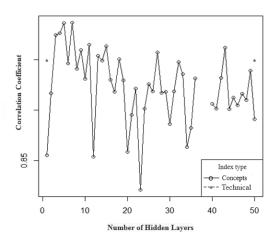


Figure 2. Correlation coefficient between predicted and actual data

This paper uses the nnet package in R to carry out the simulation experiments, and the BP neural network is created with 10 inputs and one output. The maximum times of training is 1000 and the target precision is 10^{-5} .

114 4. Analysis and Results

4.1. Use BP regression neural network to predict the opening price of the next day

After the BP neural network training is completed, the test data is used to test the predictive power of the neural network. The criterion is the relative error between the output value and the actual value calculated by the neural network from the feature vector:

$$RelativeErrorr = \frac{|PredictedData - ActualData|}{ActualData}$$
(17)

	BP nerual network by using R language
	preindex<-read.table("D:nextdayopen.txt",header=T)
step1	normalize<-function(x)return((x-min(x))/(max(x)-min(x)))
	pre.norm<-as.data.frame(lapply(preindex,normalize))
	#Import and normalize the data.
	n<-dim(pre.norm)[1]
	set.seed(13)
step2	train_index<-sample(1:n,round(n*0.8))
	train<-pre.norm[train_index,]
	test<-pre.norm[-train_index,]
	#Set 80% of the trading day data for training, while the remainder to test the accuracy of the network.
	library(nnet)
	r<-1/max(abs(train[,1:10]))
	for(i in 1:50)
	set.seed(101)
step3	$model <-nnet (Y \sim X1 + X2 + X3 + X4 + X5 + X6 + X7 + X8 + X9 + X10, data = train, size = i, rang = r, decay = 1E-5, maxit = 1000, range = 12, range = r, decay = 12, range = r, decay$
	pred_test<-predict(model,test[,1:10])
	cov<-cor(test[,11],pred_test)
	cov[i]<-cov
	#The i represents the number of hidden layers in the network.
	#The correlation coefficient between the predicted data and the test data helps us get the best i.
	set.seed(101)
step4	$model <-nnet (Y \sim X1 + X2 + X3 + X4 + X5 + X6 + X7 + X8 + X9 + X10, data = train, size = 5, rang = r, decay = 1E-5, maxit = 1000, range = 12, range $
	pred_test<-predict(model,test[,1:10])
	#We found that 5 hidden layers works best.
	preindex\$Y
	maxY<-max(preindex\$Y)
	minY<-min(preindex\$Y)
step5	test.real<-test[,11]*(maxY-minY)+minY
	t.r<-as.matrix(test.real)
	pred_test.real<-pred_test*(maxY-minY)+minY
	pt.r<-as.matrix(pred_test.real)
	#Anti-normalize the predicted data.
	wucha<-abs(t.r-pt.r)/t.r
	cbind(t.r,pt.r,wucha)
step6	cor(t.r,pt.r)
	mean(wucha)
	#Calculate the relative error and correlation coefficient.

The results are as follows:

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Table 2.	The results	by tec	hnical	indicators
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Primary Data	Predicted Data	Relative Error
39.11	38.94711	0.004164887
39.1	38.77864	0.008218959
39.62	38.91383	0.017823466
37.02	37.72703	0.01909854
36.7	37.48038	0.021263794
38.5	39.54442	0.027127728
48.7	47.38575	0.026986734
49.93	49.78173	0.002969631
47.5	48.12087	0.013071005
47.36	46.24841	0.023471145
43.79	43.85666	0.00152232
45.15	44.21843	0.020632842

Primary Data	Predicted Data	Relative Error
39.11	38.21203	0.022960176
39.1	39.07308	0.00068847
39.62	39.26665	0.00891839
37.02	37.97765	0.02586847
36.7	37.47494	0.021115416
38.5	38.09592	0.010495533
48.7	48.51834	0.003730131
49.93	49.52229	0.008165664
47.5	47.12746	0.007842977
47.36	45.38064	0.041793917
43.79	43.06277	0.016607228
45.15	45.84767	0.015452365

Table 3. The results by conceptual topic index

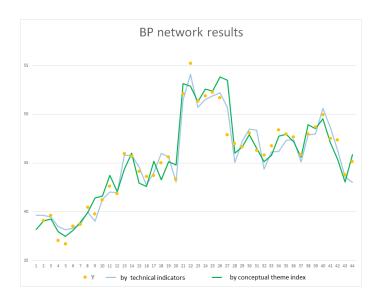


Figure 3. BP neural network results

BP neural network has a wide range of applications in nonlinear systems because of its powerful mapping and learning ability. In this prediction, the role of the BP neural network is to approximate the function. That is, to train a network approximate to the objective function through a large amount of historical data. From the plot, the prediction results of technical indicators are in a close race with that of the conceptual topic index, but the former are more accurate and consistent with the original data.

4.2. Use regression analysis to predict the opening price of the next day

Through the method of multiple linear regression, observe how the concept sector index and technical indicators affect the opening price of the next day.

¹²⁶ Using regression prediction and the concept sector index to predict the opening price of the ¹²⁷ second day is more accurate, and the predicted data is closer than the original data.

Variable	Regression Coefficients	Standard Error	t-Stat	P-value
β_0	7.759591664	3.290300309	2.358323234	0.019280566
x_1	-0.009210939	0.003165654	-2.909648366	0.004009927
x_2	0.007026998	0.002899701	2.423352805	0.016229487
<i>x</i> ₃	0.002765903	0.007028866	0.3935063	0.694346706
x_4	-0.006011439	0.002115299	-2.841885902	0.00492901
x_5	0.01754617	0.001778021	9.868371199	4.22955E-19
x_6	0.001234999	0.001905114	0.648254973	0.517531614
x_7	0.001336016	0.00818905	0.163146615	0.870560641
x_8	0.000720765	0.001473969	0.488996116	0.625357199
<i>x</i> 9	-0.004464724	0.002895185	-1.542120331	0.124557077
<i>x</i> ₁₀	0.000132717	0.001989701	0.066702106	0.946882621

Table 4. The regression results of technical indicators

Table 5. The regression results of conceptual index

Variable	Regression Coefficients	Standard Error	t-Stat	P-value
β_0	7.798106051	3.296737438	2.365401005	0.018930063
x_1	-0.009236689	0.003171453	-2.912446822	0.003977502
<i>x</i> ₂	0.007211801	0.002925265	2.465349343	0.01449783
<i>x</i> ₃	0.002265616	0.00710312	0.318960607	0.750076463
x_4	-0.006069737	0.002121746	-2.860727428	0.004657993
x_5	0.017396936	0.001802912	9.649356268	1.92266E-18
x_6	0.001320036	0.00191503	0.689303192	0.49140072
x_7	0.002086015	0.00832273	0.250640656	0.80233935
x_8	0.000755001	0.001477893	0.510863446	0.60998846
<i>x</i> 9	-0.004560978	0.002905762	-1.569632534	0.118020602
x_{10}	-4.38761E-05	0.002020424	-0.021716262	0.98269511

¹²⁸ The results are as follows:

Table 6. The results by technical indicators

Primary Data	Predicted Data	Relative Error
38.48	40.20426773	0.044809452
38.01	39.87262843	0.049003642
37.89	39.69626394	0.047671257
38.32	39.57951755	0.032868412
39.11	41.23412985	0.054311681
39.1	40.94146589	0.047096314
43.8	44.17434939	0.00854679
43.79	43.16430863	0.014288453
44.78	43.75722162	0.022840071
46.02	46.5088528	0.010622616
44.8	43.98332356	0.018229385
45.15	41.80486062	0.074089466

Primary Data	Predicted Data	Relative Error
38.48	37.84681531	0.016454903
38.01	37.75276641	0.006767524
37.89	37.92744439	0.000988239
38.32	37.44328359	0.022878821
39.11	38.14067425	0.024784601
39.1	39.17662843	0.001959806
43.8	44.44597188	0.014748216
43.79	43.55431506	0.005382163
44.78	43.31751376	0.032659362
46.02	43.8753903	0.046601688
44.8	44.95678364	0.003499635
45.15	44.07358296	0.023840909

Table 7. The results by conceptual topic index

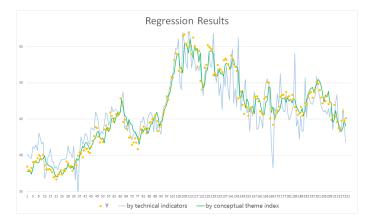


Figure 4. Regression Results

After multivariate regression analysis is performed by the data of 220 trading days, the 129 multivariate regression polynomial (ie, the objective function) is obtained, and the characteristic 130 variables are substituted into the polynomial to figure out the prediction result. The points represent 131 the actual data, and the endpoints of the polylines represent the predicted data. We can clearly see that 132 when using technical indicators as characteristic variables, the prediction results are quite different 133 from the actual values, and the adjacent points are not as coherent and smooth as the stock trend. By 134 contrast, when it comes to the conceptual topic index to which the stock belongs, the forecast result is 135 apparently more suitable. 136

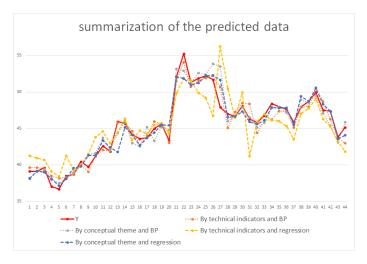


Figure 5. Summarization of the predicted data

Table 8. Accuracy analysis of four prediction methods

Prediction Methods	Correlation Coefficient	Relative Error(%)
BP network by technical indicators	0.9862409	1.29088
Regression by technical indicators	0.9012992	3.715985814
BP network by conceptual topic index	0.9590527	1.928325
Regression by conceptual topic index	0.969870007	1.869738773

According to the summary table, when the BP regression network is used for prediction, the 138 prediction error of the technical indicator is only 1.29%, while that of the conceptual topic index is 139 close to 2%. When the multiple regression model is used for prediction, the prediction error of the 140 technical indicator is high up to 3.7%, while that of the conceptual topic index is 1.87%. The technical 141 indicators are flexible and complicate calculations on the stock price, so it is applicable to the neural 142 network that can make nonlinear prediction. However, the conceptual topic index describes the aspect 143 and industry of a stock. We come to the conclusion that the trend of a stock can be observed by 144 industry and macro-economy conditions. On the whole, by introducing the technical indicators and 145 the combination of technical indicators to do predictions, it seems that BP neural network do the job 146 better, the results are the closer to the original data. 147

148 5. Conclusions

Through applying BP neural network and multiple linear regression to predict the second day opening price of 'Gree Electric Appliance', we found that both models can predict the data accurately, but, relatively speaking, BP neural network made the prediction more precisely. A stock is an unstable system with nonlinear dynamic changes, so, with its nonlinear mapping ability, BP neural network works better than multivariate linear regression models. Therefore, it had obvious advantages in the fitness, simulation and prediction of data.

In the aspect of choosing characteristic variables, the technical indicators are flexible and complicate calculations on the stock price, so it is applicable to the neural network which can make nonlinear prediction. However, neural network model needs complex computer programs to achieve desired results. Comparatively speaking, the multivariate linear regression operation is simpler to operate. To reach high-precision and stable prediction results, selecting the conceptual topic index as the characteristic variable is very worth recommending. With the expanding market capacity of China's stock market, there are varieties of technical means on trading stocks. It is an effective means of investment to choose and predict the stock by using the

¹⁶² On trading stocks. It is an enective means of investment to choose and predict the stock by dsing the

conceptual topics. The whole stock market needs the guidance and promotion of the conceptual topics.

Whether they have good prospects of development, profitability and competitiveness reveals the trend of a stock more intuitively, for the conceptual topics describes the development of the industry a stock

¹⁶⁵ of a stock more intuitively, for the conceptual topics describes the development of the industry a stock ¹⁶⁶ belongs to. Therefore, the conceptual topics of a stock cannot be ignored when we are to predict it.

Though this method may not be the most accurate, it is wise and safe to choose sustainable industries,

this is the point of 'value investment'.

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