

# **More achievements in the set theoretical model of magnetism according to the theoretical and experimental advances in material science.**

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## **Abstract:**

It has been verified theoretically the residual magnetic domains has 2 power aleph cardinality. It has also been verified theoretically that ferro para magnetic phase transitions can be explained by revision of belief mathematics. Experimentally, it has been verified nano Nd<sub>2</sub>FeB<sub>14</sub> permanent magnet has the predominant role in the mechanical properties in duplex stainless steel 2205 and magnetic composite materials. In this paper, more advances in the set theoretical model for magnetism will be achieved. Algebraic geometry will be used to achieve the equilibrium relations between the torus in euclidian space and riemannian manifold related to the torus defined in them. Tensor triangulated category will be used to discover the logical relations between the euclidian torus and riemannian manifold torus. Barkhausen effect will be explained in a new mathematical approach related to the order of cardinalities by model theory mathematics. The barkhausen effect related to Nd<sub>2</sub>FeB<sub>14</sub> materials will be mathematically approached. Landau levels will be deeply related to the prolastic functions and conditional functions.

**Key words :T3 Space-Algebraic Torus –Tensor triangulated Category –Erdos\*Rado theory-Pinning down numberpd(X)-Abelian topological groups –Lee Yang Zero- Revision of Belief -Residual magnetic domains- Heisenberg model –Ising model –Neel Lines -Barkhausen effect-Landau Levels .**

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**82B44 Disordered systems (random Ising models, random Schrödinger operators, etc.)**

## **Introduction:**

Spin models tried hard to capture the dimensionality problem of spins in Heisenberg model and Ising model. It has been verified theoretically that the residual magnetic domain has the cardinality 2 power aleph and their motion is explained by fixed brouwer theory to solve the problem of dimensionality. Also, we have used belief revision

mathematics to solve the ferro para magnetic phase transition [see Ref1, Ref2].

This new theoretical advance must be extended to explain the Barkhausen effect and Landau levels.

It will be a great deal with the torus mathematics to define an equilibrium of magnetic domain motions by algebraic topological mathematics. Tensor triangulated category will be used to describe the geometrical description of magnetic fields more precisely.

Spinodal reactions will be hindered by magnetic treatment by using lusternik schirlmen category theory in Duplex stainless steel 2205. [see Ref 3]

It will be redefined mathematically and will be proved in general formula using another experimental data found recently in Moscow university researches. [See Ref 4]

The set theoretical model that have been verified recently must be generalized to explain another phenomenological magnetic transitions. We will review the theoretical advances in the set theoretical model related to the magnetism and ferro para revision of belief mathematics in chapter 1 ,chapter 2

chapter 1 ,the set theoretical model of magnetism .

We will call the chapter 2 belief revision mathematics of ferro para transitions.

In chapter 3, we will define the equilibrium concept of magnetic domain using the mathematical torus and tensor triangulated category.

In chapter 4, the bakenhausen effect will be rexplained mathematically.

In chapter 5, the bakehausen jumps will be deeply related with the experimental advances in material science.

In chapter6, Landau levels on torus will be linked with probability functions and conditional functions.

### 1. Set theoretical model for magnetism :

In his research \*some proposition that links ferromagnetic models with cantor set theory\*, Mohamed atef has made this model to solve the dimensionality problem of Heisenberg model that consider the spins in x,y,z dimensions and Ising model that restrict the spins in z axis and he has proved that the magnetic domains has the cardinality of  $2^{\aleph_0}$  by the comparison with the Landau Lifshits model using what is proved by Danial Kapovich in the Riemannian manifold:

1. After applying and removing magnetic field  $H = 0$ , we can assume that there are magnetic domains in XYZ directions and these domains can be written as:  $[a_1, b_1] \times [a_2, b_2] \times [a_3, b_3] \subset \mathbb{R}^3$

2. These domains have the cardinality  $2^{\aleph_0}$

3. We will use the theory of invariance of dimensions which is proved by Brouwer as the domains  $[a_1, b_1] \times [a_2, b_2] \times [a_3, b_3] \subset \mathbb{R}^3$

4. Using Brouwer theory, there will be no bijection if magnetic domains  $[a_1, b_1] \times [a_2, b_2] \times [a_3, b_3] \subset \mathbb{R}^3$  are transported to z axis

5. The reason of restriction of the spins of Ising model in z axis is that there is  $T : H_{XYZ} \rightarrow H_z$

(continuous or injective). But in the case of Heisenberg Hamiltonian there will be no restriction as there is no function

6. In the case of materials that is explained by Ising model, temperature will have the concept of the function that transport magnetic domain to z – axis

7. In phase transitions that are explained only by Ising model, we can expect fractal behavior in general in these materials.

8. These fractal motions belong to space – filling curve category ( Peano, Hilbert, ..... etc ) curve will explain it.

9. Space filling curves like Hilbert Space are continuous functions will appear in Ising model materials as

11. Heisenberg model shows the spins in (  $S_x, S_y, S_z$  ), so there will be no fractal behavior in the material that exhibit phase transitions under it.

13. The phase transitions of thin films are exhibited by Ising model mainly and they cannot be explained by Heisenberg Model.

14. Summary of magnetic model, where  $d/D$  (dimension of spins / dimension of lattice)

15. We can say Ising Model can explain thin films but Heisenberg Model cannot explain thin films. Spin fluctuations are strongly dependent on temperature, so we can consider it as a tool to describe the phase transitions. The assumption of the existence of magnetic domain with cardinality ( $2^{\aleph_0}$ ) solve the problem of dimensionality of the spin models and give the proper explanation to the difference between Heisenberg model and Ising model.

We consider the case of materials that is explained by Ising model, temperature will have the concept of the function that transport magnetic domain to z – axis,  $T: H_{XYZ} \rightarrow H_z$

, so we can expect fractal motion in these materials. The fractal properties of spin clusters and boundaries which are cluster themselves are described by percolation theory. Asymptotically, cluster distributions take a general form:  $t_n \propto n^{-\tau} \exp(-\theta n)$

There is a tendency to the fractal motion in Landau Lifshits model (Henriksen, 1953; Piette & Zakrzewski, 1998; Ding & Wang, 1998). Magnetic bubbles is a small round magnetic domain induced by magnetic field in a thin film of magnetic material. Let us investigate solutions in a 2 dimensional Landau- Lifshits model. We look at Landau -Lifshits model for the anisotropic Heisenberg model when the external magnetic field is switched off  $A=0$ , the static solution is given by holomorphic functions (Jiang, 1953).

### 2. Ferro-Para magnetic phenomena by belief revision mathematics:

In his book, Set theoretical model for magnetism , Mohamed atef has linked the ferro para magnetic phenomena with the belief revision mathematics and XOR functions.

**He has demonstrated that Chiu Fan Lee\*and Neil F. Johnson clarified that the spins of Ising model is like noncooperative game.So,Nash Equilibrium is some essential concept.He has built XOR indetermined games that are consistent with his assumption of magnetic domain has the cardinality of 2 power aleph in the solution of Landau Lifshits equations.[2]**

Revision and merging differ in that the first operation is done when the new belief to incorporate is considered more reliable than the old ones; therefore, consistency is maintained by removing some of the old beliefs. Merging is a more general operation, in that the priority among the belief sets may or may not be the same. The AGM postulates for revision are:

1. Closure:  $K * P$  is a belief base (i.e., a deductively closed set of formulae);
2. Success:  $P \in K * P$
3. Inclusion:  $K * P \subset K + P$
4. Vacuity,  $\neg P \notin K$  then  $K + P$
5.  $K * P$  is inconsistent only if  $P$  is inconsistent or  $K$  is inconsistent
6. Extensionality:  $K * P = K * Q$

Let us design a model that explain the ferro -para magnetic phase transition as + operation as it transfer of magnetic domains from XYZ directions or XY direction to Z axis:from Z axis toXYZ directions and XY directions. These domains have the cardinality 2 power aleph.So it can be consider a language  $(L,+,-)$  .This model satisfy the rules of revision belief model .Postulates for conditional revision(We have supposed that magnetic phase Ferro,Para is an epistemic state):Suppose  $\Psi$  is an epistemic state and  $(B|A)$ ,  $(D|C)$  are conditionals. Let  $\Psi *(B|A)$  denote the result of revising  $\Psi$  by  $(B|A)$ .(CR0)  $\Psi *(B|A)$  is an epistemic state.

Chiu Fan Lee\*and Neil F. Johnson has showed how non-cooperative phenomena can emerge from Ising Hamiltonians, even though the individual spins behave cooperatively.They consider Ising spin models because they serve as basic models in condensed matter physics, and focus on the classical regime to avoid the complication of quantum entanglement. [40]By treating each site or subset of sites in the Ising model as a game-playing agent, we show that non-cooperative behaviour is indeed possible. In particular, we show the emergence of a prisoner's dilemma game being played' within a multi-spin system. So can macroscopic non-cooperative behavior ever arise? We now show that it can, if the subsystem under consideration has several possible configurations and hence more states from which to choose. In particular, we will search for non-cooperative phenomena in two subsystems each containing many spins. We concentrate on the specific example of non-cooperation offered by the prisoner's dilemma, since this is the only symmetric two-player two-strategy game with a unique Nash equilibrium which never coincides with the global optimum

.We start by specifying more precisely the criterion for the existence of non-cooperative behaviour. A system composed of two-body Ising Hamiltonians such as  $H = a \sum_i \uparrow_i \uparrow_{i+1} - \sum_i \uparrow_i \downarrow_{i+1} - \sum_i \downarrow_i \uparrow_{i+1} + \sum_i \downarrow_i \downarrow_{i+1}$  .

Is there a tool to express about these phenomena by Belief models and is there Depending on how beliefs are represented and what kinds of inputs are accepted, different typologies of belief changes are possible. In the most common case, when beliefs are represented by sentences in some code, and when a belief is either accepted or rejected in a belief system Kone can distinguish three main kinds of belief changes.

### **Solutions of Landau Lifshitz model in Riemannian manifold and XOR functions**

complete information models):Magnetic bubbles is a small round magnetic domain induced by magnetic field in a thin film of magnetic material.Let us investigate solutions in a 2 dimensional Landau-Lifshits model .We look at Landau -Lifshits model for the anisotropic Heisenberg modelKapovich proved the striking result :if  $M$  has a non constant holomorphic function then the ring of holomorphic function on  $M$  has a chain of prime ideals of the length of continuum(2 power aleph).

Critical properties of the Ising models on some two dimensional deterministic Sierpinski fractals with different Hausdorff measures.

Hausdorff measures are strongly related with the axiom of martin, Theorem.: Let  $s \geq 0$  and let  $H^s$  be the  $s$ -dimensional Hausdorff measure in  $n$ . The union of less than continuum many  $H^n$  negligible subsets of  $H^s$  is negligible .Søren Riis showed by using the axiom of choice ,the construction of a symmetrical and self similar subset  $A \subseteq [0, 1] \subseteq \mathbb{R}$ .

Then by an elementary strategy stealing argument it is shown that  $A$  is not determined. The (possible) existence of fractals like  $A$  clarifies the status of the controversial Axiom of Determinacy.

Definition : An infinite XOR function  $f : B^\omega \rightarrow B$  is a function with the following property: if  $hd(w_1 w_2) = 1$  then  $f(w_1) \neq f(w_2)$ .

Theorem : There exist  $2^c$  infinite XOR functions.

Theorem :No player has a winning strategy in an

infinite XOR game Gf. There is a unique functor between the chain of prime ideals and the 2<sup>co</sup>infinite XOR functions.

### 3. The equilibrium concept of magnetic domains and tensor triangulated category and Cox Particle :

Let us describe why it is so important to make an equilibrium concept of magnetic domains that have 2<sup>power aleph</sup> and the tool of tensor triangulated category.

First of all, we have solved Landau Lifshitz equations by holonomic functions when there is no applied magnetic field.

Also we have described their motion by fixed Brouwer theory

4. Using Brouwer theory, there will be no bijection if magnetic domains  $[a_1, b_1] \times [a_2, b_2] \times [a_3, b_3] \subset \square^3$  are transported to z axis

5. The reason of restriction of the spins of Ising model in z axis is that there is  $T : H_{XYZ} \rightarrow H_z$

(continuous or injective). But in the case of Heisenberg Hamiltonian there will be no restriction as there is no function

We have used the mathematical achievement of Daniel Kapovich proved the striking result: if M has a non constant holomorphic function to the complex number then the ring of holomorphic function on M has a chain of prime ideals of the length of continuum (2<sup>power aleph</sup>). So the magnetic domains that have the cardinality of 2<sup>power aleph</sup> can be redefined as M has a non constant holomorphic function to the complex number then the ring of holomorphic function on M has a chain of prime ideals of the length of continuum (2<sup>power aleph</sup>). So there are two opposite ways to describe the magnetic domains:

The first way when the magnetic domains are transferred and move  $T : H_{XYZ} \rightarrow H_z$

The second way when the magnetic domains are formed as a chain of prime ideals of the length of continuum (2<sup>power aleph</sup>) which is appear when the manifold is transferred to complex number. The first way means the transfer and the second way means the formation. There must be an equilibrium between the two different ways. When we use the tensor triangulated category to make an algebraic construction for the holonomic function hyper geometric series that are the solutions of Landau Lifshitz equations. There will be an obvious establishment for the concept of ideals. Also the tensor triangulated category will be defined after introduction for the algebraic torus. This algebraic torus is a must for studying the conserved current associated to the U(1) symmetry of a complex field related to **Klein–Gordon–Fock equation**. [see Ref 57]

**Klein Jordan equations and cox particle** will be describe well in the scope of tensor triangulated category.

The formation of magnetic domains is related to Riemannian manifold that is described by Daniel Kapovich theorems.

This Riemannian manifold can be embedded into Euclidean space **according to Nash embedding theorems**.

The **Nash embedding theorems** (or **embedding theorems**), named after John Forbes Nash, state that every Riemannian manifold can be isometrically embedded into some Euclidean space. Isometric means preserving the length of every path. For instance, bending without stretching or tearing a page of paper gives an isometric embedding of the page into Euclidean space because curves drawn on the page retain the same arclength however the page is bent. [See Ref 57]

The first theorem is for continuously differentiable ( $C^1$ ) embeddings and the second for analytic embeddings or embeddings that are smooth of class  $C^k$ ,  $3 \leq k \leq \infty$ . These two theorems are very different from each other; the first one has a very simple proof and leads to some very counterintuitive conclusions, while the proof of the second one is very technical but the result is not that surprising.

The  $C^1$  theorem was published in 1954, the  $C^k$ -theorem in 1956. The real analytic theorem was first treated by Nash in 1966; his argument was simplified considerably by Greene & Jacobowitz (1971). (A local version of this result was proved by Élie Cartan and Maurice Janet in the 1920s.) In the real analytic case, the smoothing operators (see below) in the Nash inverse function argument can be replaced by Cauchy estimates. Nash's proof of the  $C^k$ -case was later extrapolated into the h-principle and Nash–Moser implicit function theorem. A simplified proof of the second Nash embedding theorem was obtained by Günther (1989) who reduced the set of nonlinear partial differential equations to an elliptic system, to which the contraction mapping theorem could be applied.

**Theorem.** Let  $(M, g)$  be a Riemannian manifold and  $f: M^m \rightarrow \mathbf{R}^n$  a short  $C^\infty$ -embedding (or immersion) into Euclidean space  $\mathbf{R}^n$ , where  $n \geq m+1$ . Then for arbitrary  $\epsilon > 0$  there is an embedding (or immersion)  $f_\epsilon: M^m \rightarrow \mathbf{R}^n$  which is  $\square$  in class  $C^1$ ,

$\square$  isometric: for any two vectors  $v, w \in T_x(M)$  in the tangent space at  $x \in M$ ,

$$1. g(v, w) = (df_\varepsilon(v), df_\varepsilon(w))$$

$$2. \varepsilon\text{-close to } |f(x) - f_\varepsilon(x)| \leq \varepsilon \text{ [45]}$$

The Nash embedding theorem is a global theorem in the sense that the whole manifold is embedded into  $\mathbf{R}^n$ . A local embedding theorem is much simpler and can be proved using the implicit function theorem of advanced calculus in a coordinate neighborhood of the manifold. The proof of the global embedding theorem relies on Nash's far-reaching generalization of the implicit function theorem, the Nash–Moser theorem and Newton's method with postconditioning. The basic idea of Nash's solution of the embedding problem is the use of Newton's method to prove the existence of a solution to the above system of PDEs. The standard Newton's method fails to converge when applied to the system; Nash uses smoothing operators defined by convolution to make the Newton iteration converge: this is Newton's method with postconditioning. The fact that this technique furnishes a solution is in itself an existence theorem and of independent interest. There is also an older method called Kantorovich iteration that uses Newton's method directly (without the introduction of smoothing operators). The motion of magnetic domain and its transfer is described by Brouwer theory on euclidian spaces .  $[a_1, b_1] \times [a_2, b_2] \times [a_3, b_3] \subset \square^3 T : H_{XYZ} \rightarrow H_z$  , So we have two euclidian spaces one of them is the euclidian space of formation which is well defined by Nash embedding theorem of Daniel Kapovich Riemannian manifold and the second is the euclidian space of transfer. To achieve the precise description of the formation and transfer of magnetic domains , we must use the tensor triangulate category. This can be achieved by defining the algebraic torus.

In mathematics, an **algebraic torus** is a type of commutative affine algebraic group. These groups were named by analogy with the theory of *tori* in Lie group theory (see Cartan subgroup). [See Ref 61]

Tori are of fundamental importance in the theory of algebraic groups and Lie groups and in the study of the geometric objects associated to them such as symmetric spaces and buildings. If  $F$  is a field then the *multiplicative group* over a field  $F$  is the algebraic group  $G_m$  such that for any field extension  $E/F$  the group is isomorphic to the group  $E^*$ . Let  $F$  be a field with algebraic closure  $\bar{F}$ . Then a  $F$  *torus* is an algebraic group defined over  $F$  which is isomorphic over  $\bar{F}$  to a finite product of copies of the multiplicative group. Over any algebraically closed field there is up to isomorphism a unique torus of any given rank. Over the field of real numbers  $\square$  there are exactly (up to isomorphism) two tori of rank 1: the split torus  $\square^*$ .

So let us define the algebraic torus on euclidian space related to Nash Embedding and related to the fixed Brouwer theory. **torus embedding** is an algebraic variety containing an algebraic torus as an open dense subset, such that the action of the torus on itself extends to the whole variety. **Toric variety** over any field are **Cohen–Macaulay Ring**.

$$F : \square^3 \xrightarrow{\text{related to Nash embedding and magnetic domain information}} \square^3 \xrightarrow{\text{related to Brouwer theory and magnetic domain motion}}$$

Where  $F$  is a functor.

We have established above the algebraic torus and the concept of toric variety, we have also verified the existence of magnetic domain and their hypergeometric and holonomic characteristic. So, we can use what is called tensor triangulated category to achieve the geometrical concept of magnetic domains. A **Gorenstein ring** is a commutative Noetherian ring such that each localization at a prime ideal is a Gorenstein local ring, as defined above. A Gorenstein ring is in particular Cohen–Macaulay.

$CM(R)$  is a triangulated category if  $R$  is Gorenstein. Let  $\text{Spec} R$  denote the prime ideal spectrum of  $R$ , that is, the set of prime ideals of  $R$ , and let  $\text{Sing} R$  denote the singular locus of  $R$ , that is, the set of prime ideals  $\mathfrak{p}$  of  $R$  such that the local ring  $R_{\mathfrak{p}}$  is singular. Main Theorem. (1) Let  $R$  be an abstract hypersurface local ring (i.e., the completion of  $R$  is isomorphic to  $S/(f)$  for some complete regular local ring  $S$  and some element  $f$  of  $S$ ). Then one has the following one-to-one correspondences:

$$\begin{aligned} & \{ \text{thick subcategories of } CM(R) \} \\ & \uparrow \text{Supp}^{-1} \quad \text{Supp} \downarrow \\ & \{ \text{specialization-closed subsets of } \text{Spec} R \text{ contained in } \text{Sing} R \} \end{aligned}$$

(2) Let  $R$  be an  $n$ -dimensional Gorenstein singular local ring with residue field  $k$  which is locally an abstract hypersurface on the punctured spectrum. Then one has the following

$\{\text{thick subcategories of } CM(R) \text{ containing } \Omega(k)\}$

$\uparrow \text{Supp}^{-1} \text{Supp} \downarrow$

$\{\text{nonempty specialization-closed subsets of } \text{Spec} R \text{ contained in } \text{Sing} R\}$  [See54]

In his paper, Mohamed Atef has verified his theoretical assumptions by what is verified experimentally in Nd<sub>2</sub>FeB<sub>14</sub> and what is achieved by Antenna scientists to achieve the Hilbert fractal motion.

Also the spectra that is verified by Daniel Kapovich can be comparable by the  $\text{Spec} R$  of the previous tensor triangulated category.

The torsion group expresses the fractal motion of this magnetic domains.

**Theorem.** Let  $R = K[X_1, \dots, X_{N+1}]$  be the polynomial ring in  $N+1$  variables over an algebraically closed field  $K$  of characteristic zero. Suppose that  $F \in R$  defines a reduced hypersurface  $A$  with isolated singularities in the affine space  $\mathbb{A}_K^{N+1}$ . Let

$$J = \left( \frac{\partial F}{\partial X_1}, \dots, \frac{\partial F}{\partial X_n} \right)$$

denote the Jacobian ideal, let  $I := (J; F)$  denote the ideal defining the singular locus  $\text{Sing}$

(A) in  $\mathbb{A}_K^{N+1}$ . Then the following conditions are equivalent:

(a) The torsion module  $\text{Torsion}(\Omega_{A/K}^N)$  is a cyclic  $A$ -module

(b)  $\dim(\Omega_{A/K}^N)$  is a maximal

The fractal motion of magnetic domain can be described by this  $n^{\text{th}}$  syzygy between

$$F : \square^3_{\text{related to Nash embedding and magnetic domain information}} \rightarrow \square^3_{\text{related to Brouwer theory and magnetic domain motion}}$$

The symbol  $\text{Supp}$ , which we call the stable support, is a support for the stable category of Cohen-Macaulay modules.

$$\rightarrow^{\partial_{n+1}} F_{n+1} \rightarrow^{\partial_n} F_n \rightarrow^{\partial_{n-1}} F_{n-1} \rightarrow \dots \rightarrow F_1 \rightarrow F_0 \rightarrow M$$

be a minimal free resolution of  $M$

1. The  $n^{\text{th}}$  syzygy of  $M$  is defined as the image of the map  $\partial_n$  and we denote it by  $\Omega^n M$

2. The (Auslander) transpose of  $M$  is defined as the cokernel of the map  $\text{Hom}_R(\partial; R)$ .

Now, let us describe the cox particles and Klein-Gordon-Fock equation by the common rules of algebraic torus.

The algebraic torus is deeply related with the compact form, which can be realised as the unitary group  $U(1)$  or as the special orthogonal group  $SO(2)$ . It is an anisotropic torus. As a Lie group it is also isomorphic to the 1-torus  $T^1$  which is where the designation of diagonalisable algebraic groups as tori comes from.

The conserved current associated to the U(1) symmetry of a complex field  $\phi(x) \in \mathbb{C}$  satisfying the Klein Gordon equation

$$\partial_\mu J^\mu(x) = 0, J^\mu(x) = \phi^*(x) \partial^\mu \phi(x) - \phi(x) \partial^\mu \phi^*(x)$$

So there is a key word between the algebraic torus and Klein –Gordon equations that is called unitary group U(1).

The algebraic torus is deeply related with cohen maccaulay hyper surface as we have defined in the tensor triangulated category.

Also, **Klein Gordon equation** is deeply related with cox particles and their solutions can be comparable with analytical rings and functorial characteristics.

K.V. KAZMERCHUK, E.M. OVSIYUK gives a precise description for Cox’s Particle in a Magnetic Field in the Spherical Riemann Space In the cylindric coordinate system of a spherical Riemann

space (for little  $r$  and  $z$ , the metric coincides with the known one in the Minkowski space)  $dS^2 = dt^2 - \cos^2 z$

( $\int dr^2 + \sin^2 r d\varphi^2$ ) –  $dz^2$ , An analog of the uniform magnetic field is given by the

$$\text{relations } A_\phi = B \rho^2 (\cos r - 1), F_{r\phi} = B \rho \sin r$$

We have established that magnetic domains are formed in  $\mathbb{R}^3$  and their motion is described by brouwer theory as fractals

move.[seeRef57]. Then we have established functorial relation between what is embedded in  $\mathbb{R}^3$  by nash embedding and the  $\mathbb{R}^3$  by

$$F : \mathbb{R}^3 \text{ related to Nash embedding and magnetic domain information} \rightarrow \mathbb{R}^3 \text{ related to Brouwer theory and magnetic domain motion}$$

Then we described fractal motion by  $n^{\text{th}}$  syzygy .

So, the best description for Cox’s Particle in a Magnetic Field in the Spherical Riemann Space in this functorial relation that uses the term of cohen maccaulay hypersurface is what is described by analytical rings and their geometrical characteristics have a high similarity index with Cox’s Particle in a Magnetic Field in the Spherical Riemann Space.

As the motion has been described by  $n^{\text{th}}$  syzygy ,so we can consider it as finitely generated. The magnetic domain can be described as ideal and is very related with the theme of spectra and ideals. The radial equation is solved exactly in hypergeometric functions, but the equation in the  $z$ -variable can be examined qualitatively.

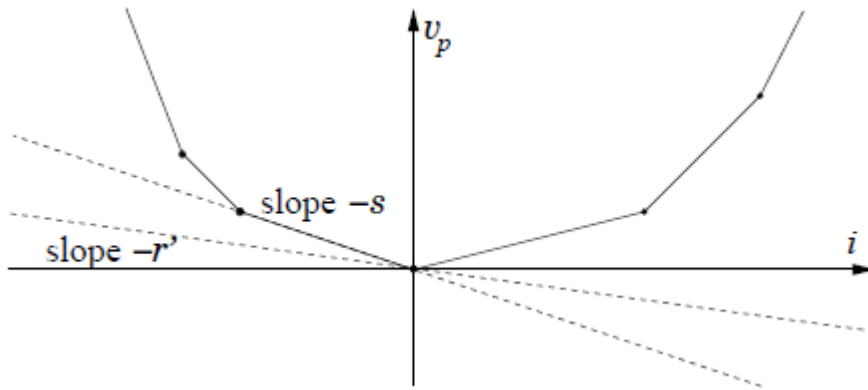
Definition. A domain is called a Bezout ring when every finitely generated ideal is principal. [See Ref58]

The motion of magnetic domain can be parameterized by valuation field .A valued \_eld is an algebraic extension  $K$  of  $k((t))$  We

$$\text{put } \Gamma^k = \left\{ \sum_{i \in \mathbb{N}} x_i u^i \right\} \text{ is a discrete valuation ring, which is complete for the } \pi \text{ adic}$$

topology.  $x \in \Gamma_{con}^K / \pi \Gamma_{con}^K$  and show that  $x$  is invertible  $\Gamma_{con}^K$ . The uniform magnetic field that is described by K.V.

KAZMERCHUK, E.M. OVSIYUK can be summeriazied as newoton polygon in this figure below.



An analog of the uniform magnetic field is given by the relations  $A_\phi = B \rho^2 (\cos r - 1)$ ,  $F_{r\phi} = B \rho \sin r$  can be compared with the newton polygon can be compared with the graph and  $\sin, \cos$  of the newton polygon.

This comparison comes from the similarity index for algebraic torus and klein Jordan equations related to the  $U(1)$ . The magnetic domain have 2 power aleph .An important theme in computable model theory is the study of computable models of complete firstorder theories. More precisely, given a complete firstorder theory  $T$ , one would like to know which models of  $T$  have computable copies and which do not. A special case of interest is when  $T$  is an  $\aleph_1$ -categorical theory. In this paper we are interested in computable models of  $\aleph_1$ -categorical theories, and we always assume that these theories are not  $\aleph_0$ -categorical. In addition, since we are interested in computable models, all the structures in this paper are countable. We assume that all languages we consider are computable.

After making a countable partitioning for the magnetic domains .We can establish the nash equilibrium between the functorial relation

$$\text{of } F : \aleph^3 \text{ related to Nash embedding and magnetic domain information } \rightarrow \aleph^3 \text{ related to Brouwer theory and magnetic domain motion}$$

By this theorem: If  $M$  and  $N$  are countable, then thesecond player has a winning strategy in  $G_\omega(M, N)$  if and only if  $M \sim N$ .

#### 4. Barkhausen effect and partitioning of magnetic domains to topological spaces:

Roland Roeder in his research\*The Ising model for magnets and the mysterious Lee-Yang zeros\* showed the deep relations between magnetism and discountinuous jumps .

He showed also the importance of LY Zeros and partionning in the magnetic phase transitions. [see Ref94,95 and 96]

This tough result is so related with what is proved by Mohamed atef as he showed that residual magnetic domains has 2 power aleph power.

Using Brouwer theory ,he showed the magnetic phase transitions and the discountinuity term importance in magnetic domain motions .

Now we link the partition that is enlighthed by LY Zeros with the set theoretical partitions of magnetic domains.

The **Barkhausen effect** is a name given to the noise in the magnetic output of a ferromagnet when the magnetizing force applied to it is changed. Discovered by German physicist Heinrich Barkhausen in 1919, it is caused by rapid changes of size of magnetic domains (similarly magnetically oriented atoms in ferromagnetic materials). Barkhausen's work in acoustics and magnetism led to the discovery, which became the main piece of experimental evidence supporting the domain theory of ferromagnetism proposed in 1906 by Pierre-Ernest Weiss. The Barkhausen effect is a series of sudden changes in the size and orientation of ferromagnetic domains, or microscopic clusters of aligned atomic magnets (spins), that occurs during a continuous process of magnetization or demagnetization. When an external magnetizing field through a piece of ferromagnetic material is changed, for example by moving a magnet toward or away from an iron bar, the magnetization of the material changes in a series of discontinuous changes, causing "jumps" in the magnetic flux through the iron. These can be detected by winding a coil of wire around the bar, attached to an amplifier and loudspeaker. The sudden transitions in the magnetization of the material produce current pulses in the coil, which when amplified produce a sound in the loudspeaker. This makes a crackling sound, which has been compared to candy being unwrapped, Rice Krispies, or the sound of a log



fire. This sound, first discovered by German physicist Heinrich Barkhausen, is called **Barkhausen noise**. Similar effects can be observed by applying only mechanical stresses (e.g. bending) to the material placed in the detecting coil. y pinned between two points A and B. For  $X$  a set and  $\lambda, \kappa$  cardinals, we let  $[X]^\kappa$  be the collection of all subsets with cardinality  $\kappa$ . We call  $f : [X]^\kappa \rightarrow \lambda$  a partition of  $[X]^\kappa$ . We say  $X \subseteq Y$  is homogeneous for the partition  $f$ ,  $\alpha \prec \lambda, f(A) = \alpha$  [See65]

We must again mention we have proved that magnetic domains has the cardinality of  $2^{\aleph_1}$ .

We can partition the magnetic domains to sets with less cardinality by Erdos Rado theory:

**Erdos – Rado theorem :**  $\delta_n(\kappa)^+ \rightarrow (\kappa^+)_\kappa^{n+1}$  [See Ref66]

These sets can be formed topological spaces with small cardinalities less than  $2^{\aleph_1}$

We can explain the barkhausen effect by this partitioning as when we partition the magnetic domains of  $2^{\aleph_1}$  we can verify that magnetic domains can be changed and then the bakehausen effect is produced.

Now we must explain the bake hausen jumps also by this theory:

The pinning down number  $pd(X)$  of a topological space  $X$  is the smallest cardinal  $\kappa$  such that for any neighborhood assignment

$U : X \rightarrow \tau_X$ , there is a set  $A \in [X]^\kappa$  with  $A \cap U(x) \neq \emptyset$  for all  $x \in X$

Let us mention that we can express the bakehausen jumps as a variation on the pinning down number  $pd(X)$  [See 64]

As it can be different from jump to jump and can be written in the form of different cardinalities. In a metric space, the separation between two points is quantified very precisely- by the metric. It is not so in any topological space. The separation axioms,  $T_1 \dots T_6$  characterize the *degree of separation* between two points in a topological space.  $T_{3.5}$  is a degree of separation "in between"  $T_3$  and  $T_4$ . Therefore, let us go through  $T_3$  and  $T_4$  before  $T_{3.5}$ . [See65]

$T_3$  stands for *regular hausdorff*: Every pair of points can be separated by disjoint open sets and a point and a closed set can also be separated by disjoint open sets.

$T_4$  stands for *normal hausdorff*: Every pair of points can be separated by disjoint open sets and every pair of closed sets can also be separated by disjoint open sets.

Separation by disjoint open sets is one way of separating. Now there is a big qualitative difference between  $T_3$  and  $T_4$ , that is given by the Urysohn's lemma. It says that in a  $T_4$  space, for any pair of disjoint closed sets, one can define a continuous function from the space to  $[0,1]$  that takes the value 0 in one of the closed sets and 1 in the other.

It seems, two closed sets in a  $T_4$  space are *so separated* that a function can continuously drop from 1 to 0 between them. This is a different degree of separation than separation by open sets- it is called separation by a continuous function. Therefore, the natural question is, is a similar theorem true about regular spaces?. Can we separate a point and a closed set in a  $T_3$  space by a continuous function? The answer is no.

A point and a closed set in a  $T_3$  space are *not separated enough* for a function to fall from 1 to 0 between them; Therefore there must be an intermediate between  $T_3$  and  $T_4$  where points and closed sets *start* to be separated by a function. Therefore we define  $T_{3.5}$  as the intermediate axiom.

$T_{3.5}$  stands for *Tychonoff*: A closed set and a point not in it can be separated by a function; i.e., one can define a continuous function with codomain  $[0,1]$  such that it takes the value 0 at the point and 1 in the closed set. Sometimes it is called  $T_\pi$

We can regulate the magnetic domains to be  $T_\pi$  I think it is so easy to make a topological regulation for the magnetic domains . The motion of magnetic domain and its transfer is described by brouwer theory on euclidian spaces .

$[a_1, b_1] \times [a_2, b_2] \times [a_3, b_3] \subset \mathbb{R}^3 : H_{XYZ} \rightarrow H_z$ , So we have two euclidian spaces one of them is the euclidian space of formation which is well defined by nash embedding theorem of daniel kapovich riemannian manifold and the second is the euclidian space of transfer. In his paper, Mohamed Atef has verified his theoretical assumptions by what is verified experimentally in  $Nd_2FeB_{14}$  and what is achieved by Antena scientists to achieve the Hilbert fractal motion .Also the spectra that is verified by Daniel kapovich can be comparable by the Spec  $\mathbb{R}$  of the previous tensor triangulated category. The torsion group expresses the fractal motion of this magnetic domains .

Riemannian manifold in itself can be treated as hausdorff space. High rank set theoretical topologist Danial Kaspovich have verified his results by ZFC axioms which is in consistent with the axiom of determinacy. So if we want to make a revision of belief model it must be

a complete information model by XOR functions. Let  $B = \{0, 1\}$ . For two words  $v, w \in B^\omega$ , where  $m \leq \omega$ , let  $hd(v, w) = |\{i : v_i \neq w_i\}|$  be the Hamming distance between  $v$  and  $w$ . For  $v, w \in B^\omega$ , we let  $v \sim_i w$  if  $hd(v, w) < i$ .

Definition: An infinite XOR function  $f: B^\omega \rightarrow B$  is a function with the following property: if  $hd(w_1 w_2) = 1$  then  $f(w_1) \neq f(w_2)$ .

Theorem: There exist  $2^c$  infinite XOR functions.

Theorem: No player has a winning strategy in an infinite XOR game  $G_f$ . There is a unique functor between the chain of prime ideals and the  $2^c$  infinite XOR functions.

So the pinning down number for  $T\pi$  regulation of magnetic domain of 2 power aleph is deeply related to the partitioning theorems of Erdős and Radon.

If  $X$  is a  $T_{3.5}$ -space, then  $F(X)$  and  $A(X)$  denote the free topological group and the free abelian topological group on  $X$ .

$F(X)$  is a topological group containing (a homeomorphic copy of)  $X$  such that

1.  $X$  generates  $F(X)$  algebraically,
2. every continuous function  $f: X \rightarrow H$ , where  $H$  is any topological group, can be extended to a continuous homomorphism  $\bar{f}: F(X) \rightarrow H$ . Similarly for  $A(X)$ . The existence of these groups was proved by Markov.

Theorem (JvMSSz) Let  $X$  be a  $T_{3.5}$ -space. Then  $d(X) = d(F(X)) = d(A(X))$ . If  $X$  is neat, then so are  $A(X)$  and  $F(X)$ , and  $pd(X) = pd(A(X)) = pd(F(X))$ .

**By the partitioning of  $T_{3.5}$ -space into small groups by Erdős-Rado theorem into small cardinalities.**

**We can use these partitioned  $T_{3.5}$ -space to create a generated free abelian groups  $Y$ . After that, we can regulate this pinning number by  $gp_n(Y, e)$  is the set of words of length not exceeding  $n$  in the subgroup generated.**

In recent years, Eli Katz, S.A. Morris and Peter Nicolas have investigated the question of which free abelian topological groups can be embedded as subgroups of the free abelian topological group on the closed unit interval  $I$  and, more generally, the closed ball  $B^n$ , for positive integers  $n$ . [See 67 and 68]

**Definition.** If  $X$  is a topological space with distinguished point  $e$ , the abelian topological group  $F(X)$  is said to be the (Graev) free abelian topological group on  $X$  if (a)  $X$  is a subspace of  $F(X)$ , and

(b) any continuous map  $f$  from  $X$  into any abelian topological group  $H$ , sending  $e$  to the identity of  $H$ , extends uniquely to a continuous homomorphism  $\bar{f}: F(X) \rightarrow H$ .

**Theorem A** (Mack et al.) Let  $Y = UY$ , be any  $k$ -space with distinguished point  $e$ . Then  $F(X)$  is a  $k$ -space and  $F(Y)$  has  $km$ -decomposition  $F(Y) = U \cup gp_n(Y, e)$ , where  $gp_n(Y, e)$  is the set of words of length not exceeding  $n$  in the subgroup generated by  $Y$ . [See 67 and 68]

**Definition.** Let  $Y = UY$ , be a  $k$ -space, and let  $Z = UZ$ , be a closed  $k$ -subspace of  $F(X)$ . Then  $Y$  is said to be regularly situated with respect to  $X$  if for each natural number  $n$  there is an integer  $m_n$  such that  $gp_n(Y) \cap gp_m(X) \subseteq gp_{m_n}(Y)$ .

**Theorem B** (Mack et al.) Let  $F(X)$  is a  $km$ -space, and  $Y$  is a closed subset of  $F(X)$  containing  $e$  such that  $Z \setminus \{e\}$  is a free algebraic basis for  $gp(Z)$  and  $Z$  is regularly situated with respect to  $Y$ , then  $gp(Z)$  is  $F(Z)$ .

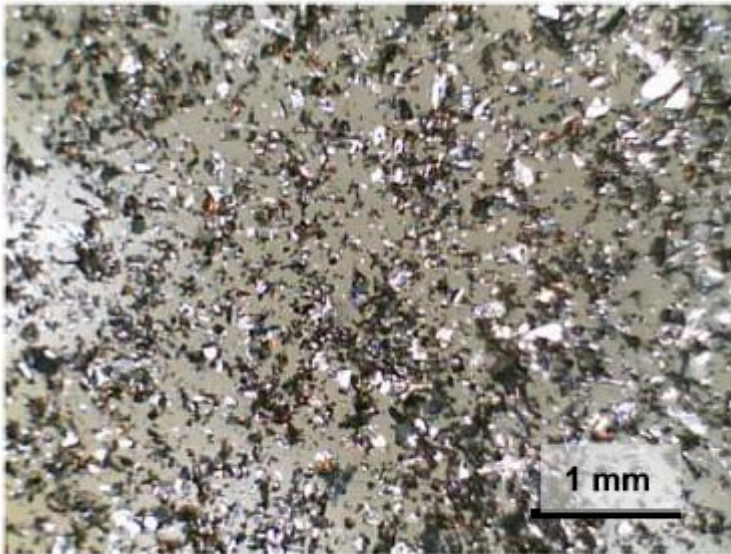
Let  $T$  be a  $L$ -theory with infinite model. For any  $\kappa \geq |L| + \aleph_1$ , there is  $N$   $T$  of cardinality  $\kappa$  with  $2^\kappa$  automorphisms.

So the pinning structures can be saved in all the partition methodologist into different finite cardinals.

### 5. Barkhausen jumps according to the advances in experimental material science:

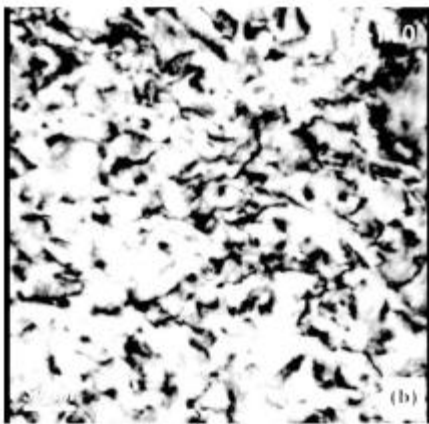
In the absence of an external magnetic field the magnetic moments of the soft magnetic filler particles are close to zero. Thus, the ME materials have no net magnetization and in static experiments (static shear, elongation or compression) demonstrate usual elastic behavior characterized by linear Hookean stress-strain dependence at small strains. We have synthesized recently ME based on hard magnetic particles of NdFeB alloy. In contrast to ME filled with carbonyl iron or magnetite, magnetically hard magnetic elastomers (MHME) have non-zero magnetization in the absence of external magnetic field and demonstrate the striking properties which MSME acquire only in a magnetic field. In particular, the preliminary studies have shown that being pre-magnetized MHME are characterized by a strain independent modulus and demonstrate the shape memory effect. Besides, we have found a strong magnetodielectric effect in MHME displayed as 150% increase of effective dielectric permittivity in the magnetic field of 10 kOe. Thus, these materials could be used in

numerous applications in various areas and understanding of their behavior in magnetic field is challenging. we analyze in details the influence of the magnetizing field on the magnetic and viscoelastic properties of MHME based on NdFeB powder of different particle size and concentration. The NdFeB and carbonyl iron powders were used as magnetic fillers. To study the influence of magnetic particle size on the ME properties the two types of NdFeB powders were chosen with the average particle sizes of 50  $\mu\text{m}$  and 2  $\mu\text{m}$ . The image of the NdFeB particles is presented in figure 1. Carbonyl iron particles have the average size of 3  $\mu\text{m}$ . [See Ref4]



**Figure 1.** The optical microscopy image of NdFeB particles.

It is proved that there was many enhancing in the surface energy of this composite. In his paper heat treatment of duplex stainless steel 2205 by inserting nano Nd<sub>2</sub>FeB<sub>14</sub> in HIP manifold, Mohamed atef succeeded to verify experimentally that the impact energy increased from 20-25J to be 100 Joule after applying magnetic field and solve the problem of losing impact energy during aging treatment of duplex stainless steel 2205. [See Ref3]



**Fig 2:** Aged  $\square$ -ferrite grain after impact test after inserting Nd<sub>2</sub> Fe B<sub>14</sub> particles in HIP manifold and the application of high magnetic field

**Mohamed Atef has used Lusternik Schnirelman category in his paper to formulate the thermal content OF DUPLEX STAINLESS 2205 .The same mathematics can be extended to cover The NdFeB and carbonyl iron powders. [See Ref3,4]**

**DEFINITION.** The Lusternik-Schnirelman category of A in X,  $\text{cat}(A; X)$ , is the least integer n such that A can be covered by n closed subsets of X each of which is contractible in X. If no such integer n exists we put  $\text{cat}(A; X) = \infty$ . We define  $\text{cat}(X) = \text{cat}(X; X)$

The Lusternik-Schnirelman category is used for finslers spaces especially. As we mentioned above, solobev space where Ising model and cahn hillard equations are highly related to it. Solobev space is suppoed to be defined on finsler manifold (Antonelli, Ingarden, & Matsumoto, 2013; Bao, Chern, & Shen, 1996).Using the MAIN THEOREM OF LUSTERNIK-SCHNIRBLMANTHEORY,we can write the entire thermal content of the system as  $CT(M) = \square D(c(m))E(c(n))$ [See Ref3]  
 $D(c(m))$  is fractal measurement depends on  $c(m)$  as defined in main theorem of Lusternik Schnirbl main theory  $E(c(n))$  is dipolar field interaction depends on  $c(n)$  as defined in main theory of lusternik schinirby main theorem.

We must mention that Mohamed atef work was deeply related with dislocation dynamics and their properties that has been changed after magnetic filling Nd2FeB14 in HIPed duplex stainless steel 2205.

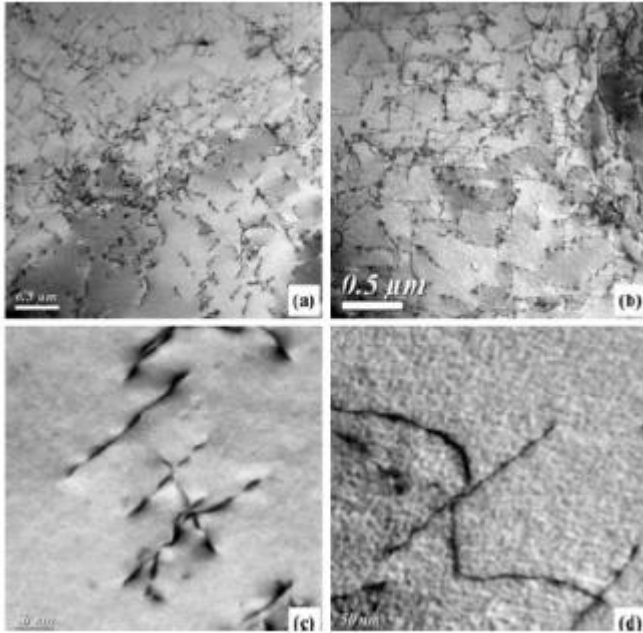


Fig 3: Transmission electron micrographs of the: (a) unaged  $\alpha$ -ferrite; (b) aged  $\alpha$ -ferrite; (c) unaged  $\alpha$ -ferrite with high magnification; (d) aged  $\alpha$ -ferrite with higher magnification

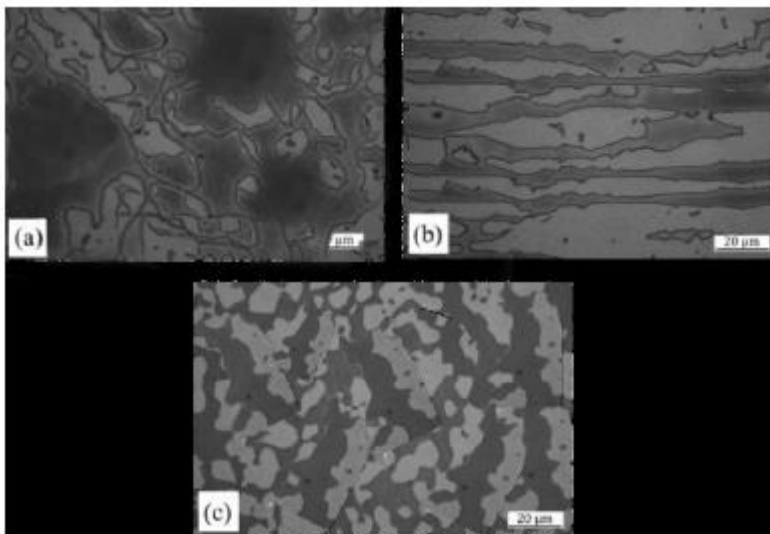


Fig 4:Optical micrographs of the 2205 duplex stainless steel bar after inserting Nd2Fe B14 particles in HIP manifold.(dislocation densities vary considerably) : (a) transverse section of the unaged specimen; (b) longitudinal section of the unaged specimen; (c) transverse section of the aged specimen

A new theory of Barkhausen jumps is proposed, which depicts the movement of 180° Bloch walls as due to kinks bounded by Néel lines. [See Ref 70] These lines can be pinned on dislocations. Two activation energies are introduced, one of them for small jumps in low fields and low temperatures (pinning energy), the other one for line nucleation energy. An expression of the coercive field is given. After-effect phenomena can be explained by the same physical processes. Comparison is made with recent experiments. It is suggested that the variation in size of Barkhausen jumps with field partially reflects the short-range order of pinning defects, and also a change in behaviour with the density of Néel lines (flexible when they behave independently one from the other, rigid when they interact).

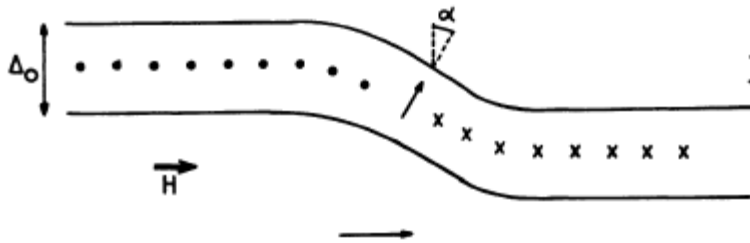


Figure 5: The displacement of the wall segment on the left under the action of applied magnetic field  $H$ . The line energy increases by a quantity of the order. [See Ref 70]

This new theory that is proposed is deeply related with our characteristic structures for duplex stainless steel 2205 and NdFeB and carbonyl iron powders.

So, We can make a common formula for the surface energy that is related to LS category and T3 space that is related with barkhausen effect and the foliation. There is only one partition for T3 Space such that: Every Borel set of the first category in T3 space is nowhere dense and the support of each regular borel measure on T3 is nowhere dense. Then we introduce two versions of the tangential category for a measurable lamination. For a space  $X$  which are new even  $F$  is the underlying measurable lamination of a (topological) lamination. The first one, simply called its (LS) category, is a direct adaptation to measurable laminations of the tangential (or even the usual) category. The second one is called the  $\Lambda$ -category because it involves a transverse invariant measure  $\Lambda$ , whose existence is a restriction.

Proposition :

Let  $T$  be a measurable transversal which meets each leaf at most in one point. Then  $\Lambda(T) \leq \text{Cat}(F, \Lambda)$  [See Ref 71,72,76]

Proposition : Let  $(X, F, \Lambda)$  be a measurable lamination with a transverse in-variant measure. If  $(X, F)$  is a measurable suspension  $f: M \times h \rightarrow S$ , then  $\text{Cat}(F, \Lambda) \leq \text{Cat}(M) \cdot \Lambda(S)$

Proposition : For a manifold and a standard Borel space  $T$ , let  $M \times T$  be foliated as a product. Then

$\text{Cat}(M \times T, \Lambda) = \text{Cat}(M) \cdot \Lambda(T)$  for every measure  $\Lambda$  on  $T$ , considered as an invariant measure of  $M \times T$ . [See Ref 71,72,76]

## 6. Set theoretical model for Landau Levels on torus and probability functions:

Here is an apparent paradox here: infinitesimal translations should be associated to canonical operators  $[p_x, p_y] \propto i \hbar B$ , and, at the same time, live in a Landau level of finite dimension  $B = L_1 L_2 / (hc/e)$ , which is impossible from Wintner's theorem.

Let  $T^2 = \square^2 / \square^2$  denote the two-torus; we describe it in physical terms by identifying an atlas of four local charts specified as follows:

1.  $U_\alpha = \{0 < x < L_1, 0 < y < L_2\}$
2.  $U_\beta = \{x < x < L_1 + \bar{x}, 0 < y < L_2\}$
3.  $U_\gamma = \{0 < x < L_1, y < y < L_2 + \bar{y}\}$
4.  $U_\delta = \{x < x < L_1 + \bar{x}, y < y < L_2 + \bar{y}\}$

with some choice of constants  $\bar{x}$  and  $\bar{y}$ . A uniform magnetic field  $B$  transverse to the surface  $T^2$  is represented by the translation invariant two-form  $B = B dx \wedge dy$

$A_\beta(x, y) = A_\alpha(x, y) (\bar{x} < x < L_1)$   $A_\gamma(x, y) = A_\alpha(x, y) (\bar{y} < y < L_2)$

$A_\delta(x, y) = A_\alpha(x, y) (\bar{x} < x < L_1, \bar{y} < y < L_2)$   $A_\beta(x + L_1, y) = A_\alpha(x, y) + d(.5B(L_1 y - L_2 x))$ . Markov processes are stochastic processes that have the property that the next value of the process depends on the current value, but it is conditionally independent of the previous values of

the stochastic process – in other words, the behavior of the process in the future is stochastically independent of its behavior in the past, given the current state of the process. For a stochastic process to be a Markov process, it must have this property, which is referred to as the **Markov property**.

**It is deeply related with landau levels. When we define the landau levels in torus, we mean that there is a deep meaning of convexity. [See Ref90]**

**So to calculate the probability of a particle to occupy landau levels, you must calculate it in hitting property .**

**Uwe Basal [See 91,92]** obtain symmetric formulae for the probabilities that a plane convex body hits exactly 1, 2, 3, 4, 5 or 6 triangles of a lattice of congruent triangles in the plane. Furthermore, a very simple formula for the expectation of the number of hit triangles is derived.

In the following, we choose  $\phi$  as the angle between the direction perpendicular to the sides b and segment  $\sigma$  (see Fig. 7). We assume that for every angle  $\phi$ ,  $0 \leq \phi \leq 2\pi$ , there is a position of the reference point O so that C with angle  $\phi$  denoted as  $C_\phi$  is entirely contained in exactly one triangle T of  $\mathbb{R}^2$ ; b; c.

$$c^*(\phi) = s(\phi) \csc \alpha + s(\phi + \alpha + \beta) \csc \beta + s(\phi + \alpha + \pi)(\cot \alpha + \cot \beta) .$$

.....(1)

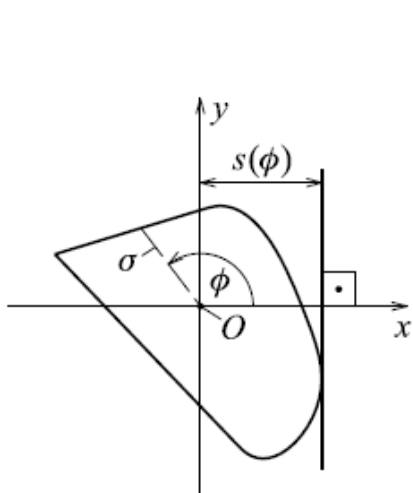


Fig7:Support function s

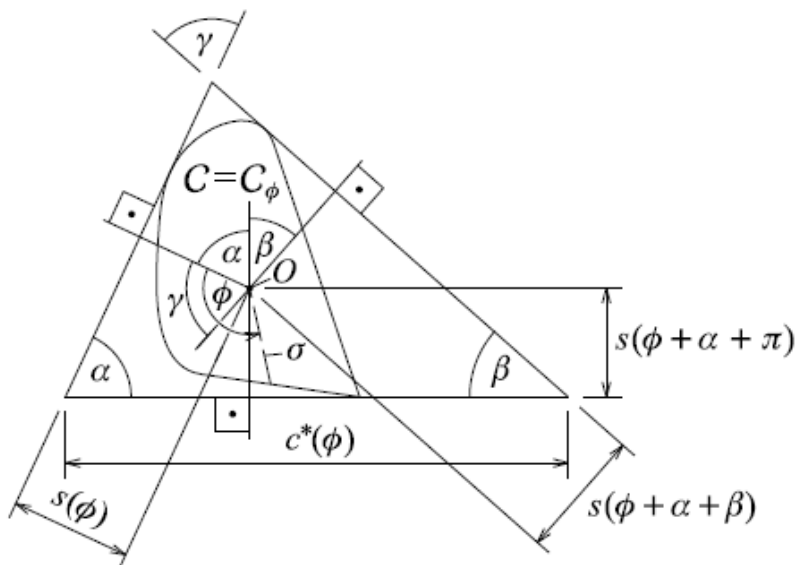


Figure8:Trinagle(  $\phi$  )

**These triangulation formula and their probabilistic field is deeply related to two things :**

- 1.Tensor triangulated category approach for magnetic fields on torus conditions.**
- 2.The propabilty nature of landau levels as they donot related with a specific laws in the case of torus and deeply related with probability. [See91]**

The best probalistic interruption when the relation (1) holds followed by this in the next page .And also we give the randomness of particle distribution by Z number related with landau levels.

If you practice the equations you will find they are deeply related with the uniform distribution in figure 6 even if in the E(Z)formula . In figure 6 ,we have partitioned them into N with different scales.

Also we we have calculated p(1),p(2),.....,p(6).[See91,92] **These triangulation formula and their probabilistic field is deeply related to two things :**

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$$p(1) = 1 - \frac{(a + b + c)u}{\pi Q} + \frac{(a^2 + b^2 + c^2)J(0)}{2\pi Q^2} + \frac{bcf_1(\alpha) + caf_1(\beta) + abf_1(\gamma)}{\pi Q^2},$$

$$p(2) = \frac{(a + b + c)u}{\pi Q} - \frac{3(a^2 + b^2 + c^2)J(0)}{2\pi Q^2} - \frac{bcf_2(\alpha) + caf_2(\beta) + abf_2(\gamma)}{\pi Q^2},$$

$$p(3) = \frac{3(a^2 + b^2 + c^2)J(0)}{2\pi Q^2} + \frac{bcf_3(\alpha) + caf_3(\beta) + abf_3(\gamma)}{\pi Q^2},$$

$$p(4) = \frac{bcJ(\alpha) + caJ(\beta) + abJ(\gamma)}{\pi Q^2} - \frac{(a^2 + b^2 + c^2)J(0)}{2\pi Q^2} - \frac{F}{Q},$$

$$p(5) = 0, \quad p(6) = \frac{F}{Q},$$

with

$$f_1(x) = I(x) - J(x), \quad f_2(x) = 2I(x) - 3J(x), \quad f_3(x) = I(x) - 3J(x),$$

$$I(x) = \int_0^\pi w(\phi)w(\phi + x) d\phi, \quad J(x) = \int_0^{2\pi} s(\phi)s(\phi + x) d\phi,$$

and the expectation for the random number  $Z$  of hit triangles by

$$E(Z) = 1 + \frac{(a + b + c)u}{\pi Q} + \frac{2F}{Q}.$$

Donot forget the probability function related to landau levels in finite dimensions has been solved as follow:

$$\psi_\nu(z) = \mathcal{N}_\nu e^{\frac{1}{2}z^2 + 2\pi i\nu z/L_1} \sum_{n=-\infty}^{\infty} \exp\{-(z + nL_1/N + i\nu L_2/N)^2\}.$$

$$\rho_N(z) = \sum_\nu |\psi_\nu(z)|^2$$

And the density matrix with  
So you can partition the density to  $N=1,2,\dots,\dots,6$

Also donot forget we define them in torus and it is easy to obtain probability distribution in convex body.

In his book ,Gabriele Isberner [See93]described rules for conditional states and it is also the best way to describe the problem of landau levels in torus as we have mentioned it is impossible from Wintner's theorem.In his work ,he described the conditional functions as a solution of the problem of nonmonotonicity [See Ref 93]. Donot forget that there is a high monotonic behavior for the charged particles to occupy landau levels.Also ,we have proved that magnetic domains have the cardinality of 2 power aleph and we can regulate them to  $k$  - ordinals . Also donot forget we define them in torus and it is easy to obtain probability distribution in convex body.

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**Theorem 4.2.1.** *The conditional revision operator  $*$  satisfies (CR5) iff for each epistemic state  $(\Psi, \leq_{\Psi})$  and for each conditional  $(B|A)$  it holds that:*

$$\omega \leq_{\Psi} \omega' \quad \text{iff} \quad \omega \leq_{\Psi*(B|A)} \omega' \quad (4.1)$$

*for all worlds  $\omega, \omega'$  both being elements of  $Mod(AB)$  (or of  $Mod(A\bar{B})$ , or of  $Mod(\bar{A})$ , respectively).*

As an immediate consequence, equation (4.1) yields

**Lemma 4.2.1.** *Suppose (4.1) holds for all worlds  $\omega, \omega'$  both being elements of  $Mod(AB)$  (or of  $Mod(A\bar{B})$ , or of  $Mod(\bar{A})$ , respectively). Let  $E \in \mathcal{L}$  be a proposition such that either  $E \leq AB$ , or  $E \leq A\bar{B}$ , or  $E \leq \bar{A}$ . Then*

$$\min(E; \Psi) = \min(E; \Psi * (B | A))$$

**Lemma 4.3.1.** *Let  $(B|A)$  be a conditional in  $(\mathcal{L} | \mathcal{L})$ , let  $\kappa$  be an ordinal conditional function. The following three statements are equivalent:*

- (i)  $\kappa \models (B|A)$ .
- (ii)  $\kappa(AB) < \kappa(A\bar{B})$ .
- (iii)  $\kappa(\bar{B}|A) > 0$ .

[See93]So, we have the mathematical tools like set theory to solve the problem of landau levels on torus as the ordinals for landau levels. [See90]

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