Analysis of the Behavior of Kurtosis by Simplified Half Triangle Model and its Application to Machine Diagnosis

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Abstract

Among many dimensional and dimensionless amplitude parameters, Kurtosis (4-th normalized moment of probability density function) is recognized to be the sensitive good parameter for machine diagnosis. Kurtosis has a value of 3.0 under normal condition and the value generally goes up as the deterioration proceeds. But there are cases that kurtosis value goes up and then goes down when damages increase as time passes. In this paper, a simplified calculation method of kurtosis is introduced for the analysis of impact vibration with one sided affiliated impact vibration which occurs towards the progress of time. That phenomenon is often watched in the failure of such as bearings' outer race. One sided affiliated impact vibration is approximated by one sided triangle towards the progress of time and simplified calculation method is introduced. By varying the shape of triangle, various models are examined and above phenomenon is traced and its reason is clarified by the analysis. As peak value grows up, Kurtosis increases, then after the damage spread to other rolling elements, the width of the signal shape spread and

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Kurtosis falls. When the peak value arises after that, Kurtosis rises up again. Such movement can be confirmed. For the generalization, plural cases of different rolling element numbers are compared. Utilizing this method, the behavior of kurtosis is forecasted and analyzed while watching machine condition, and correct diagnosis is executed.

Mathematics Subject Classification : 60G35

Keywords: impact vibration, Kurtosis, deterioration, rolling element

1 Introduction

In mass production firms such as steel making that have big equipments, sudden stops of production processes by machine failure cause great damages such as shortage of materials to the later processes, delays to the due date and the increasing idling time.

To prevent these troubles, machine diagnosis techniques play important roles. So far, Time Based Maintenance (TBM) technique has constituted the main stream of the machine maintenance, which makes checks for maintenance at previously fixed time. But it has a weak point that it makes checks at scheduled time without taking into account whether the parts still keeping good conditions or not. On the other hand, Condition Based Maintenance (CBM) makes maintenance checks by watching the condition of machines. Therefore, if the parts are still keeping good condition beyond its supposed life, the cost of maintenance may be saved because machines can be used longer than planned. Therefore the use of CBM has become dominant. The latter one needs less cost of parts, less cost of maintenance and leads to lower failure ratio.

However, it is mandatory to catch a symptom of the failure as soon as possible of a transition from TBM to CBM is to be made. Many methods are developed and examined focusing on this subject. In this paper, we propose a method for the early detection of the failure on rotating machines which is the most common theme in machine failure detection field.

So far, many signal processing methods for machine diagnosis have been proposed [1]. As for sensitive parameters, Kurtosis, Bicoherence and Impact Deterioration Factor (ID Factor) were examined [2, 4-6, 11]. In this paper we focus our attention on the index parameters of vibration. Kurtosis is one of the sophisticated inspection parameters which calculates normalized 4th moment of Probability Density Function (PDF). But these methods have to be calculated using computer which cannot be easily available at the maintenance site. Kurtosis has a value of 3.0 under normal condition and the value generally goes up as the deterioration proceeds. But there were cases that kurtosis values went up and then went down when damages increased as time passed which were observed in our experiment in the past [6, 7].

In this paper, a simplified calculation method of kurtosis is introduced for the analysis of impact vibration with one sided affiliated impact vibration which occurs towards the progress of time. That phenomenon is often watched in the failure of such as bearings' outer race. One sided affiliated impact vibration is approximated by triangle and simplified calculation method is introduced. By varying the shape of triangle, various models are examined and above phenomenon is traced and its reason is clarified by the analysis. For the generalization, plural cases of different rolling element numbers are compared. Utilizing this method, the behavior of kurtosis is forecasted.

In the field of plant maintenance, there are often the cases that data should be handled in an easy manner and machine diagnosis should be done speedily. In those fields, the proposed method enables failure detection of the equipment in an easy way. Such research can not be found as long as we have searched. The proposed method enables sensitive machine diagnosis by a simple method. It takes less cost than those of the previous methods presented before. This method would be applicable in many data handling fields. Finding and examining such a new field would be a great issue in the near future.

The rest of this study is organized as follows. We survey each index of deterioration in section 2. Simplified calculation method of Kurtosis including affiliated impact vibration is stated in section 3. Past experimental data are explained in section 4. Numerical example is exhibited in section 5. Section 6 is a summary.

2 Factors for Vibration Calculation

In cyclic movements such as those of bearings and gears, the vibration grows larger whenever the deterioration becomes bigger. Also, it is well known that the vibration grows large when the setting equipment to the ground is unsuitable [11]. Assume the vibration signal is the function of time as x(t). And also assume that it is a stationary time series with mean 0. Denote the probability density function of these time series as p(x). Indices for vibration amplitude are as follows.

$$X_{root} = \left[\int_{-\infty}^{\infty} |x|^{\frac{1}{2}} p(x) dx\right]^{2}$$
(1)

$$X_{rms} = \left[\int_{-\infty}^{\infty} x^2 p(x) dx\right]^{\frac{1}{2}}$$
(2)

$$X_{abs} = \int_{-\infty}^{\infty} |x| p(x) dx$$
(3)

$$X_{peak} = \lim_{n \to \infty} \left[\int_{-\infty}^{\infty} x^n p(x) dx \right]^{\frac{1}{n}}$$
(4)

These are dimensional indices which are not normalized. They differ by machine sizes or rotation frequencies. Therefore, normalized dimensionless indices are required. There are four big categories for this purpose.

- A. Normalized root mean square value
- **B**. Normalized peak value
- C. Normalized moment
- D. Normalized correlation among frequency domain
- A. Normalized root mean square value
 - a.Shape Factor : SF

$$SF = \frac{X_{rms}}{\overline{X}_{abs}}$$
(5)

 $(\overline{X}_{abs} : \text{mean of the absolute value of vibration})$

B. Normalized peak value

b.Crest Factor : CrF

$$CrF = \frac{X_{peak}}{X_{rms}} \tag{6}$$

(X_{peak} : peak value of vibration)

c.Clearance Factor : ClF

$$ClF = \frac{X_{peak}}{X_{root}} \tag{7}$$

d.Impulse Factor : IF

$$IF = \frac{X_{peak}}{\overline{X}_{abs}}$$
(8)

e.Impact Deterioration Factor : ID Factor

$$ID = \frac{X_{peak}}{X_c} \tag{9}$$

(X_c : vibration amplitude where the curvature of PDF becomes maximum)

C. Normalized moment

f. Skewness: SK

$$SK = \frac{\int_{-\infty}^{\infty} x^3 p(x) dx}{\left[\int_{-\infty}^{\infty} x^2 p(x) dx\right]^{\frac{3}{2}}}$$
(10)

g.Kurtosis : KT

$$KT = \frac{\int_{-\infty}^{\infty} x^4 p(x) dx}{\left[\int_{-\infty}^{\infty} x^2 p(x) dx\right]^2}$$
(11)

D. Normalized correlation in the frequency domain

h.Bicoherence

Bicoherence means the relationship of a function at different points in the frequency domain and is expressed as :

$$Bic_{,_{XXX}}(f_1, f_2) = \frac{B_{_{XXX}}(f_1, f_2)}{\sqrt{S_{_{XX}}(f_1) \cdot S_{_{XX}}(f_2) \cdot S_{_{XX}}(f_1 + f_2)}}$$
(12)

Here

$$B_{xxx}(f_1, f_2) = \frac{X_T(f_1) \cdot X_T(f_2) \cdot X_T^*(f_1 + f_2)}{T^{\frac{3}{2}}}$$
(13)

means Bispectrum and

$$X_{T}(t) = \begin{cases} x(t) (0 < t < T) \\ 0 (else) \end{cases}$$

T : Basic Frequency Interval

$$X_T(f) = \int_{-\infty}^{\infty} X_T(t) e^{-j2\pi f t} dt$$
(14)

$$S_{xx}(f) = \frac{1}{T} X_T(f) X_T^*(f)$$
(15)

Range of Bicoherence satisfies

$$0 < Bic_{,xxx}(f_1, f_2) < 1$$
 (16)

When there exists a significant relationship between frequencies f_1 and f_2 , Bicoherence is near 1 and otherwise comes close to 0. These indices are generally used in combination and machine condition is judged totally. Among them, Kurtosis is said to be a superior index [3] and many researches on this have been made [2, 4, 5]. Judging from the experiment we made in the past, we may conclude that Bicoherence is also a sensitive good index [6, 7].

In [2], ID Factor is proposed as a good index. In this paper, we focusing on the indices of vibration amplitude, a simplified calculation method of Kurtosis including affiliated impact vibration is introduced.

3 Simplified Calculation Method of Kurtosis

3.1 Several Facts on Kurtosis

KT may be transformed into the one for discrete time system as :

$$KT = \frac{\int_{-\infty}^{\infty} x^4 p(x) dx}{\left[\int_{-\infty}^{\infty} x^2 p(x) dx\right]^2}$$

=
$$\lim_{N \to \infty} \frac{\frac{1}{N-1} \sum_{i=1}^{N} (x_i - \overline{x})^4}{\left\{\frac{1}{N-1} \sum_{i=1}^{N} (x_i - \overline{x})^2\right\}^2}$$
(17)

Where

$$\{x_i\}: i = 1, 2, \cdots, N$$

are the discrete signal data.

 \overline{x} is an average of $\{x_i\}$

$$\overline{x} = \frac{1}{N} \sum_{i=1}^{N} x_i$$

Here the variance, the mean, KT of N amount of data are stated as

$$\sigma_N^2$$
, \overline{x}_N , KT_N

3.2. Simplified Calculation Method of Kurtosis

When there arise failures on bearings or gears, peak value arises cyclically. In the early stage of the defect, this peak signal usually appears clearly. Generally, defects will injure other bearings or gears by contacting the inner covering surface as time passes. When defects grow up, affiliated impact vibration arises. One sided affiliated impact vibration which occurs towards the progress of time occurs in the case that there is a failure of such as bearings' outer race [12]. See Chart 1.

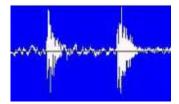


Chart 1. Example of one sided affiliated impact vibration

These signals can be approximated by triangle model. Hereafter, we analyze these cases by utilizing simplified model. Assume that the peak signal which has p times magnitude from normal signals arises during m times measurement of

samplings. Here m is a number of rolling element. As for determining sampling interval, sampling theorem is well known [10]. But in this paper, we do not pay much attention on this point in order to focus on our proposal theme. Suppose that affiliated vibration can be approximated by triangle and set sampling count as d, then we can assume following triangle model (Figure 1).

When d = 1, the peak signal which has p times magnitude from normal signals arises.

When d = i, the peak signal which has $p - (i-1)\frac{p-1}{q}$ times magnitude from nor mal signals arises $(i = 1, \dots, q)$.

When $d \ge q+1$, normal signal.

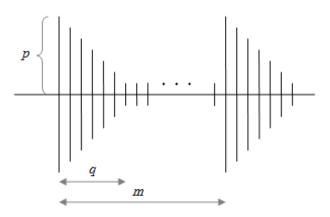


Figure 1. Impact vibration and affiliated vibration

Let σ_N^2 state as $\overline{\sigma}_N^2$ when impact vibration occurs. As to 4th moment and Kurtosis, let them state as $\overline{MT_N}(4)$, $\overline{KT_N}$ in the same way.

 $\overline{\sigma}_N^2$ can be calculated as follows.

$$\overline{\sigma}_{N}^{2} = \frac{1}{m-1} \sum_{i=1}^{m} (x_{i} - \overline{x})^{2}$$

$$= \left[\sum_{i=1}^{q} \left\{ p - (i-1) \frac{(p-1)}{q} \right\}^{2} \right] \frac{\sigma_{N}^{2}}{m-1} + (m-1-q) \frac{\sigma_{N}^{2}}{m-1}$$

$$= \sigma_{N}^{2} + \frac{\sigma_{N}^{2}}{m-1} (q+1)(p-1) \left\{ 1 + \frac{(p-1)(2q+1)}{6q} \right\}$$
(18)

as for $\overline{MT_N}(4)$, utilizing :

$$\sum_{i=1}^{n} i^{3} = \left\{ \frac{n(n+1)}{2} \right\}^{2}$$
$$\sum_{i=1}^{n} i^{4} = \frac{n}{30} (n+1)(2n+1)(3n^{2}+3n-1)$$

 $\overline{MT_N}(4)$ can be calculated as follows.

$$\overline{MT_{N}(4)} = \frac{1}{m-1} \sum_{i=1}^{m} (x_{i} - \overline{x})^{4}$$

$$= \frac{1}{m-1} \left[\sum_{i=1}^{q} \left\{ p - (i-1) \frac{(p-1)}{q} \right\}^{4} \right] MT_{N}(4) + \frac{m-1-q}{m-1} MT_{N}(4)$$

$$= \left[1 + \frac{1}{m-1} (q+1)(p-1) \cdot R \right] MT_{N}(4)$$
(19)

Here,

$$R = \frac{1}{30}(p-1)^3 \frac{1}{q^3}(2q+1)(3q^2+3q-1) + (p-1)^2 \frac{1}{q}(q+1) + (p-1)\frac{1}{q}(2q+1) + 2$$
(20)

Then we get $\overline{KT_N}$ as :

$$\overline{KT_{N}} = \frac{\left\{1 + \frac{1}{m-1}(q+1)(p-1)R\right\}KT_{N}}{\left[1 + \frac{1}{m-1}(q+1)(p-1)\left\{\frac{2q+1}{6q}(p-1) + 1\right\}\right]^{2}}$$
(21)

Here we introduce the following number. Each index is compared with normal index as follows.

$$F_a = \frac{P_{abn}}{P_{nor}}$$

Here,

P_{nor} : Index at normal condition

P_{abn} : Index at abnormal condition

We get F_a as :

$$F_{a} = \frac{\overline{KT_{N}}}{KT_{N}}$$

$$= \frac{1 + \frac{1}{m-1}(q+1)(p-1)R}{\left[1 + \frac{1}{m-1}(q+1)(p-1)\left\{\frac{2q+1}{6q}(p-1)+1\right\}\right]^{2}}$$
(22)

4 Past Experimental Data

Here, we confirm the past experimental data in order to ascertain general behavior of Kurtosis. In [4], *KT* are calculated for the bearings that have small, medium and large defects and the rotation frequency varies (Table 1).

Table 1. KT for each case

	Rotation frequency (rpm)						
	200	500	1700				
Small defect	3.5~4.0*	3.4~3.9	2.5~3.8				
Medium defect	6~7	4.6~5.6	3.8~4.6				
Large defect	7~10*	5.7~8	4~6				

*: Numerical value stated in [4], else read the score in the graph of [4].

These results can be taken into account, though the definition of defect size does not necessarily coincide.

5 Numerical Example

If the system is under normal condition, we may suppose p(x) becomes a normal distribution function. Under this condition, *KT* is always :

KT = 3.0

Under the assumption of 3.2, let m=12. Considering the case $p=1,2,\dots,6$ and q=1,2,3,4, we obtain Table 2 from the calculation of (22).

			p						
		1	2	3	4	5	6		
	1	1.0	1.459	2.773	4.328	5.702	6.789		
a	2	1.0	1.422	2.409	3.425	4.254	4.883		
q	3	1.0	1.400	2.185	2.901	3.446	3.845		
	4	1.0	1.373	2.006	2.531	2.912	3.184		

Table 2. F_a by the variation of p,q

As $KT_N \cong 3.0$, we show Table 3 as an approximation of $\overline{KT_N}$ by multiplying 3.0 for each item of Table 2.

Table 3. $\overline{KT_N}$ for each case

		р р							
		1	2	3	4	5	6		
	1	3.0	4.377	8.319	12.984	17.106	20.367		
a	2	3.0	4.266	7.227	10.275	12.762	14.649		
q	3	3.0	4.200	6.555	8.703	10.338	11.535		
	4	3.0	4.119	6.018	7.593	8.736	9.552		

As p increases, F_a and $\overline{KT_N}$ increase. On the other hand, F_a and $\overline{KT_N}$ decrease as q increases when p is the same. When damages increase or transfer to another place, peak level grows up and affiliated impact vibration spreads. This means that $\overline{KT_N}$ value shift from left-hand side upwards to right-hand side downwards in Table 3. For example, following transition of $\overline{KT_N}$ can be supposed.

When	q = 1, p = 1,	$\overline{KT_N} = 3.0$
When	q = 1, p = 2,	$\overline{KT_N} = 4.377$
When	q = 3, p = 2,	$\overline{KT_N} = 4.200$
When	q = 4, p = 3,	$\overline{KT_N} = 6.018$

We made experiment in the past [6,7]. Summary of the experiment is as follows. Pitching defects are pressed on the gears of small testing machine.

Small defect condition: Pitching defects pressed on 1/3 gears of the total gear.

Medium defect condition: Pitching defects pressed on 2/3 gears of the total gear.

Big defect condition: Pitching defects pressed on whole gears of the total gear.

RMS and Kurtosis in this case are exhibited in Table 4.

	Kurtosis	RMS
Normal	2.961	289.212
Small Defect	3.747	671.175
Medium Defect	2.970	833.592
Big Defect	3.310	855.375

Table 4. Experiment Result

RMS values grow up as damages increase. Kurtosis value responds to the damage in the small defect level. But it is rather close to normal level under medium and goes up again in big defect. We thought damages became rounded, so Kurtosis had fallen. Considering the above stated model which includes the affiliated impact vibration, we can explain the case that Kurtosis is big initially and then fall and goes up again. As peak value grows up, Kurtosis increases, then after the damage spread to other rolling elements, the width of the signal shape spread and Kurtosis falls. When the peak value arises after that, Kurtosis rises up again. Such movement can be confirmed. Though the score may differ by the adjustment of parameter, we can analyze the behavior of Kurtosis principally by utilizing this simplified model and calculation method.

We can easily calculate (20) watching the waveform at the maintenance site, and we can get much more correct estimation of Kurtosis than the method presented by [8].

Changing the variable set (p,q) by 0.1 for each variable from (0.1, 0.1) to (10.0, 10.0), following results are obtained. The variable set is picked up for the data within plus or minus 0.009 to the designated score.

	< <i>m</i> =	12>	< <i>m</i> =	=9>	<"	<i>l</i> =16>
		Kurtosis	(p,q)	Kurtosis	(p,q)	Kurtosis
Condition		value		value		value
	(p,q)	under the		under the		under the
		set (p,q)		set (p,q)		set (p,q)
Normal	(1,1)	3.000	(1,1)	3.000	(1,1)	3.000
(Experiment						
results						
:Kurtosis						
2.961)						
	(0.1,3.6)	3.751	(0.1,2.3)	3.748	(0.1,5.3)	3.749
-	(0.2,4.2)	3.746	(0.2,2.7)	3.746	(0.2,6.2)	3.747
	(0.3,5.3)	3.745	(0.3,3.4)	3.738	(0.3,5.3)	3.745
	(0.4,7.7)	3.736	(0.3,3.5)	3.756	(0.3,7.7)	3.739
_	(0.4,7.8)	3.741	(0.4,5.0)	3.739	(0.4,7.8)	3.748
_	(0.4,7.9)	3.747	(0.4,5.1)	3.748	(1.9,8.6)	3.752
	(0.4,8.0)	3.751	(0.4,7.8)	3.753	(1.9,8.7)	3.746
Small De-	(0.4,8.1)	3.756	(1.7,1.2)	3.745	(1.9,8.8)	3.740
fect	(1.7,0.5)	3.740	(1.8,3.6)	3.753		
(Experiment	(1.8,4.3)	3.755	(1.8,3.7)	3.744		
results	(1.8,4.4)	3.750	(1.9,4.8)	3.751		
:Kurtosis	(1.8,4.5)	3.745	(2.1,6.1)	3.746		
3.747)	(1.8,4.6)	3.741	(2.2,6.5)	3.747		
	(1.9,6.4)	3.756	(2.3,6.8)	3.753		
	(1.9,6.5)	3.747	(2.4,7.1)	3.746		
	(1.9,6.6)	3.739	(2.5,7.3)	3.752		
-	(2.0,7.6)	3.750	(2.6,7.5)	3.750		
-	(2.0,7.7)	3.739	(2.7,7.7)	3.742		
-	(2.1,8.4)	3.748	(2.8,7.8)	3.754		
F	(2.2,9.0)	3.747	(3.0,8.1)	3.741		

Table 5. The variable set (p,q) which is close to the value in Table 4

(2.3,9.5)	3.742	(3.1,8.2)	3.742	
(2.4,9.8)	3.755	(3.2,8.3)	3.741	
(2.4,9.9)	3.739	(3.3,8.4)	3.738	
		(3.5,8.5)	3.755	
		(3.6,8.6)	3.746	
		(3.8,8.7)	3.754	
		(3.9,8.8)	3.741	
		(4.1,8.9)	3.742	
		(4.3,9.0)	3.740	
		(4.4,9.0)	3.754	
		(4.6,9.1)	3.747	
		(4.8,9.2)	3.739	
		(4.9,9.2)	3.750	
		(5.1,9.3)	3.738	
		(5.2,9.3)	3.748	
		(5.5,9.4)	3.742	
		(5.6,9.4)	3.751	
		(5.9,9.5)	3.742	
		(6.0,9.5)	3.749	
		(6.4,9.6)	3.744	
		(6.5,9.6)	3.750	
		(6.9,9.7)	3.741	
		(7.0,9.7)	3.746	
		(7.1,9.7)	3.752	
		(7.5,9.8)	3.739	
		(7.6,9.8)	3.743	
		(7.7,9.8)	3.748	
		(7.8,9.8)	3.753	
		(8.3,9.9)	3.740	
		(8.4,9.9)	3.744	
		(8.5,9.9)	3.748	
		(8.6,9.9)	3.752	
		(8.7,9.9)	3.756	

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			(9.2,10.0)	3.740		
-			(9.3,10.0)	3.743		
			(9.4,10.0)	3.746		
-			(9.5,10.0)	3.749		
-			(9.6,10.0)	3.753		
-			(9.7,10.0)	3.756		
Medium	(0.1,0.3)	2.977	(0.1,0.3)	2.967	(0.6,0.1)	2.975
Defect	(0.6,0.1)	2.966	(0.4,9.6)	2.975		
(Experiment			(0.6,9.9)	2.976		
results						
:Kurtosis						
2.970)						
	(0.1,1.1)	3.310	(0.2,0.6)	3.304	(0.1,1.8)	3.301
-	(0.2,1.3)	3.314	(0.3,0.8)	3.317	(0.1,1.9)	3.313
-	(0.3,1.6)	3.306	(0.4,1.2)	3.310	(0.2,2.1)	3.301
-	(0.3,1.7)	3.317	(0.5,2.1)	3.307	(0.2,2.2)	3.310
	(0.4,2.3)	3.309	(0.5,2.2)	3.314	(0.3,2.7)	3.306
-	(0.4,2.4)	3.317	(0.6,4.5)	3.302	(0.3,2.8)	3.314
	(0.5,3.5)	3.302	(0.6,4.6)	3.305	(0.4,3.6)	3.302
	(0.5,3.6)	3.308	(0.6,4.7)	3.307	(0.4,3.7)	3.309
Big Defect	(0.5,3.7)	3.313	(0.6,4.8)	3.309	(0.4,3.8)	3.315
(Experiment	(0.5,3.8)	3.319	(0.6,4.9)	3.312	(0.5,5.4)	3.302
results	(1.5,0.8)	3.319	(0.6,5.0)	3.314	(0.5,5.5)	3.306
:Kurtosis	(1.5,0.9)	3.315	(0.6,5.1)	3.316	(0.5,5.6)	3.310
3.310)	(1.5,1.0)	3.312	(0.6,5.2)	3.317	(0.5,5.7)	3.314
	(1.5,1.1)	3.311	(0.6,5.3)	3.319	(0.5,5.8)	3.318
	(1.5,1.2)	3.311	(0.2,9.2)	3.313	(1.5,0.1)	3.311
-	(1.5,1.3)	3.311	(0.6,6.5)	3.319	(1.5,4.1)	3.301
	(1.5,1.4)	3.311	(0.6,6.6)	3.317	(1.5,4.2)	3.303
-	(1.5,1.5)	3.312	(0.6,6.7)	3.315	(1.5,4.3)	3.303
	(1.5,1.6)	3.313	(0.6,6.8)	3.312	(1.5,4.4)	3.304
	(1.5,1.7)	3.314	(0.6,6.9)	3.310	(1.5,4.5)	3.305
-	(1.5,1.4)	3.311	(0.6,7.0)	3.306	(1.5,4.6)	3.306

(1.5,1.5)	3.312	(0.6,7.1)	3.303	(1.5,4.7)	3.307
(1.5,1.6)	3.313	(1.5,4.3)	3.318	(1.5,4.8)	3.307
(1.5,1.7)	3.314	(1.5,4.4)	3.314	(1.5,4.9)	3.308
(1.5,1.8)	3.315	(1.5,4.5)	3.311	(1.5,5.0)	3.308
(1.5,1.9)	3.316	(1.5,4.6)	3.307	(1.5,5.1)	3.309
(1.5,2.0)	3.318	(1.5,4.7)	3.303	(1.5,5.2)	3.309
(1.5,2.1)	3.319	(1.6,6.2)	3.317	(1.5,5.3)	3.309
(1.5,5.1)	3.319	(1.6,6.3)	3.311	(1.5,5.4)	3.310
(1.5,5.2)	3.317	(1.6,6.4)	3.304	(1.5,5.5)	3.310
(1.5,5.3)	3.316	(1.7,7.1)	3.319	(1.5,5.6)	3.310
(1.5,5.4)	3.314	(1.7,7.2)	3.311	(1.5,5.7)	3.310
(1.5,5.5)	3.313	(1.7,7.3)	3.302	(1.5,5.8)	3.310
(1.5,5.6)	3.311	(1.9,8.2)	3.309	(1.5,5.9)	3.310
(1.5,5.7)	3.309	(2.0,8.5)	3.310	(1.5,6.0)	3.300
(1.5,5.8)	3.307	(2.1,8.7)	3.317	(1.5,6.1)	3.300
(1.6,8.5)	3.316	(2.1,8.8)	3.302	(1.5,6.2)	3.309
(1.6,8.6)	3.312	(2.2,8.9)	3.318	(1.5,6.3)	3.309
(1.6,8.7)	3.307	(2.2,9.0)	3.302	(1.5,6.4)	3.309
(1.6,8.8)	3.303	(2.3,9.1)	3.313	(1.5,6.5)	3.308
(1.7,9.9)	3.314	(2.5,9.4)	3.309	(1.5,6.6)	3.308
(1.7,10.0)	3.308	(2.6,9.5)	3.311	(1.5,6.7)	3.307
		(2.7,9.6)	3.312	(1.5,6.8)	3.307
		(2.8,9.7)	3.310	(1.5,6.9)	3.306
		(2.9,9.8)	3.307	(1.5,7.0)	3.306
		(3.0,9.9)	3.302	(1.5,7.1)	3.305
		(3.1,9.9)	3.317	(1.5,7.2)	3.304
		(3.2,10.0)	3.310	(1.5,7.3)	3.303
				(1.5,7.4)	3.303
				(1.5,7.5)	3.302
				(1.5,7.6)	3.301

There are 23 similar cases for small defect, 2 similar cases for medium defect and 42 similar cases for big defect.

By varying the number of rolling elements, we have obtained the following results. In m = 9, there are 59 similar cases for small defect, 3 similar cases for medium defect and 48 similar cases for big defect.

In m = 16, there are 8 similar cases for small defect, 1similar case for medium defect and 51 similar cases for big defect.

6 Conclusions

We proposed a simplified calculation method of Kurtosis for the analysis of impact vibration including one sided affiliated impact vibration. One sided affiliated impact vibration was approximated by triangle and simplified calculation method was introduced. By varying the shape of triangle, various models were examined and the phenomenon that Kurtosis went up and down as the deterioration proceeded was traced and its reason was clarified by the analysis. As peak value grows up, Kurtosis increases, then after the damage spread to other rolling elements, the width of the signal shape spread and Kurtosis falls. When the peak value arises after that, Kurtosis rises up again. Such movement could be confirmed. For the generalization, plural cases of different rolling element numbers were compared. There are 23 similar cases for small defect, 2 similar cases for medium defect and 42 similar cases for big defect.

By varying the number of rolling elements, we have obtained the following results.

In m = 9, there are 59 similar cases for small defect, 3 similar cases for medium defect and 48 similar cases for big defect.

In m = 16, there are 8 similar cases for small defect, 1 similar case for medium defect and 51 similar cases for big defect.

Utilizing this method, the behavior of Kurtosis would be forecasted and analyzed while watching machine condition and correct diagnosis would be executed. This proposed method is simple enough to be calculated even on a pocketsize calculator. The effectiveness of this method should be examined in various cases.

In the field of plant maintenance, there are often the cases that data should be handled in an easy manner and machine diagnosis should be done speedily. In those fields, the proposed method enables failure detection of the equipment in an easy way. Proposed method enables sensitive machine diagnosis by a simple method. It takes less cost than those of the previous methods presented before. This method would be applicable in many data handling fields. Finding and examining such a new field would be a great issue in the near future.

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